

Stellar Wind Theory



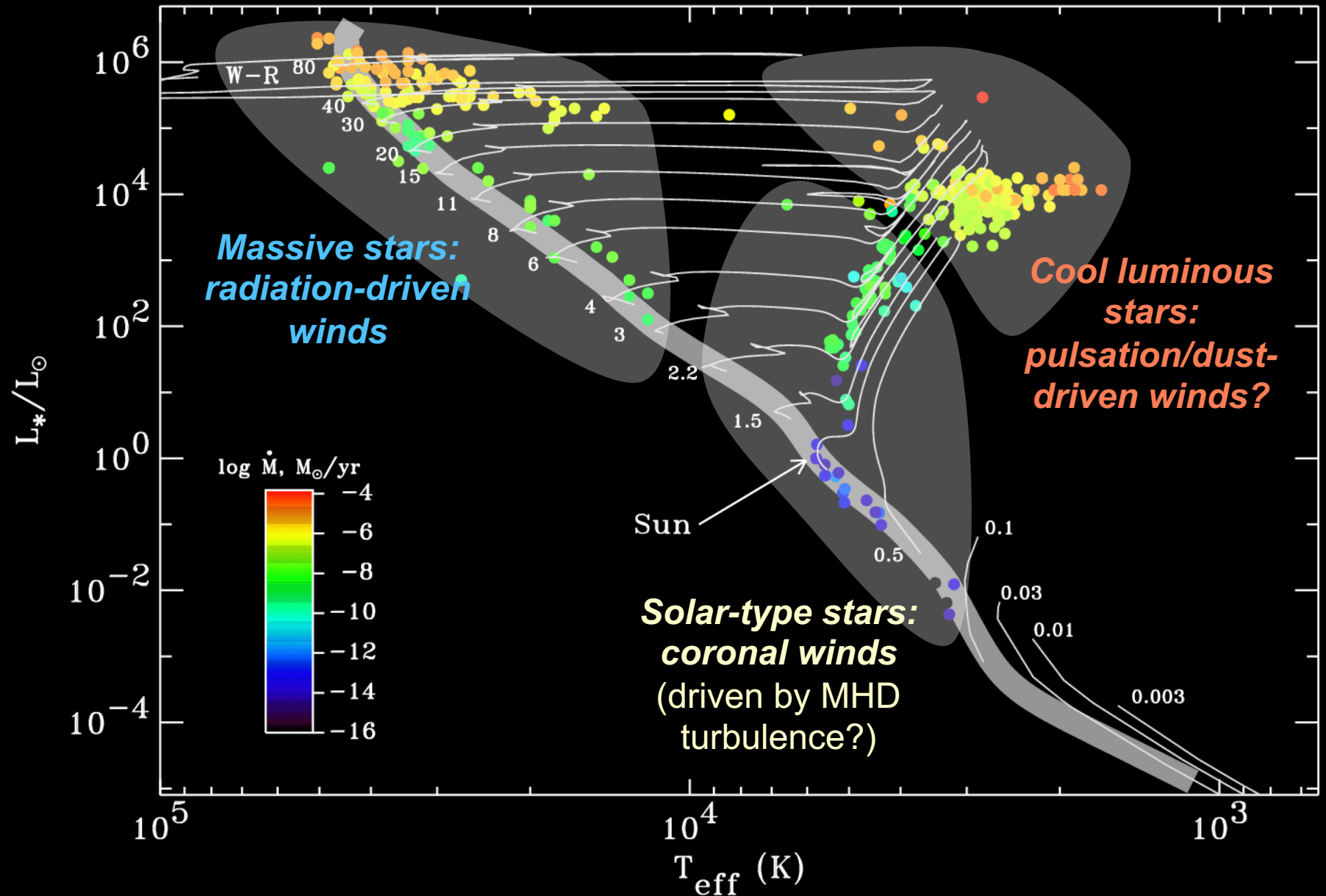
Steven R. Cranmer

Harvard-Smithsonian Center for Astrophysics

with A. van Ballegooijen, S. Saar, A. Dupree, N. Brickhouse, et al.



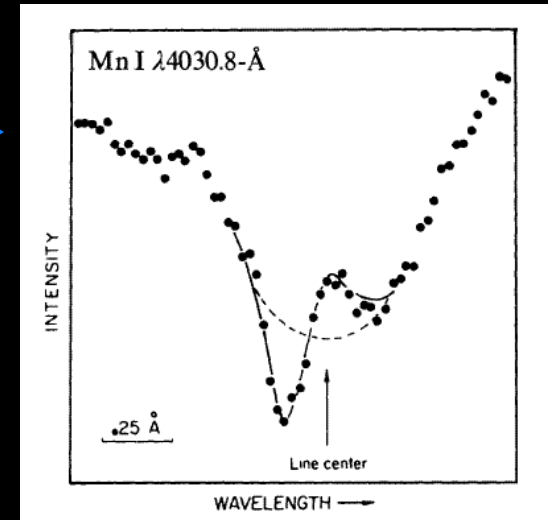
Stellar winds across the H-R Diagram



Traditional diagnostics of mass loss

- **Optical/UV spectroscopy:** either blueshifted absorption or full “P Cygni” profiles.
- **IR continuum:** circumstellar dust causes SED excess.
- **Molecular lines (mm, sub-mm):** CO, OH masers.
- **Radio:** free-free emission from (partially ionized?) components of the wind.
- Continuum methods need V_∞ from another diagnostic to get mass loss rate.

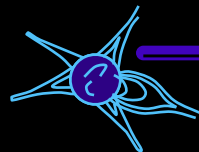
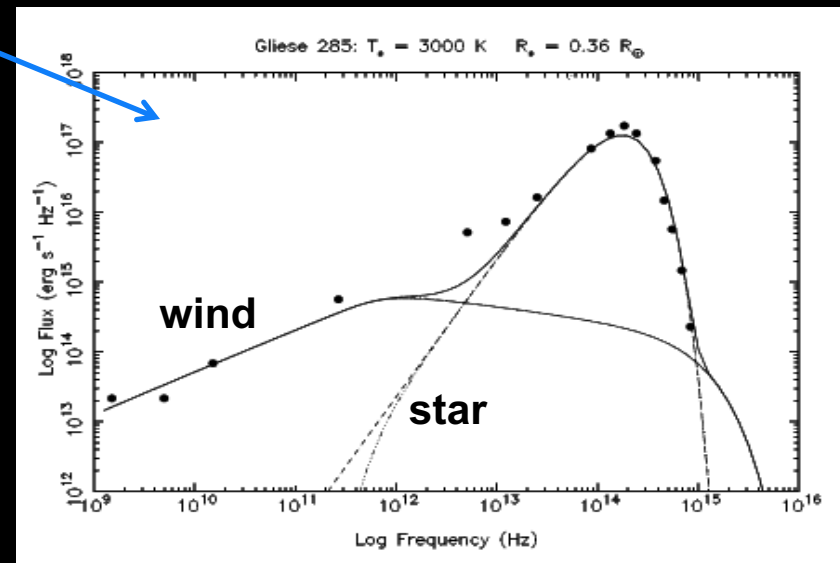
(Bernat 1976)



$$\dot{M}_{(\text{dust, molec, ion})} < \dot{M}_{\text{total}}$$

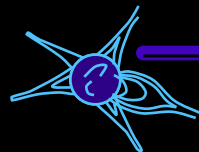
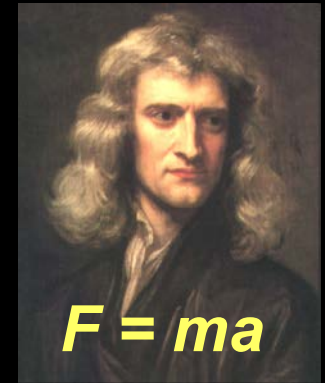
• Clumping?

(van den Oord & Doyle 1997)

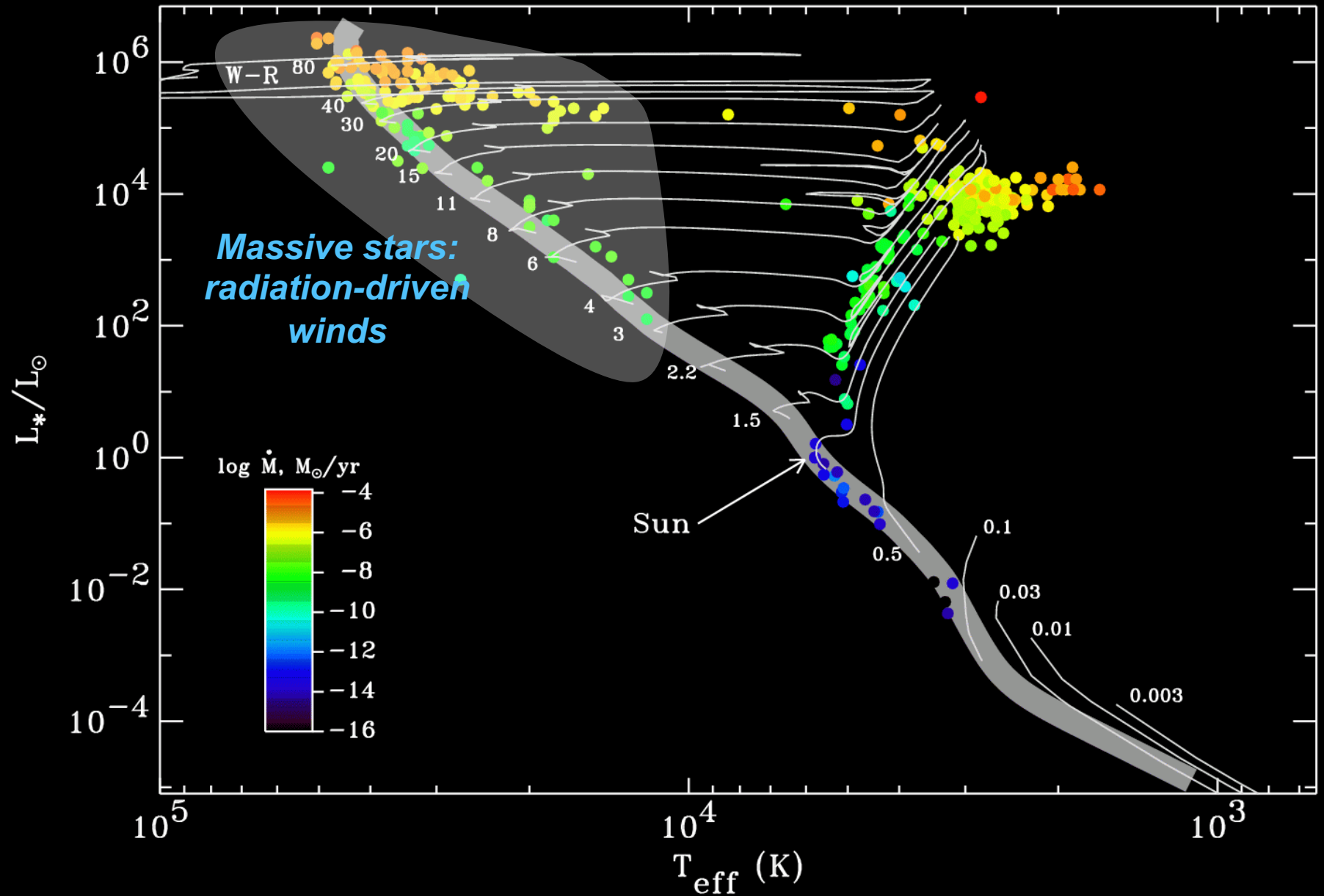


Driving a stellar wind

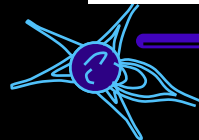
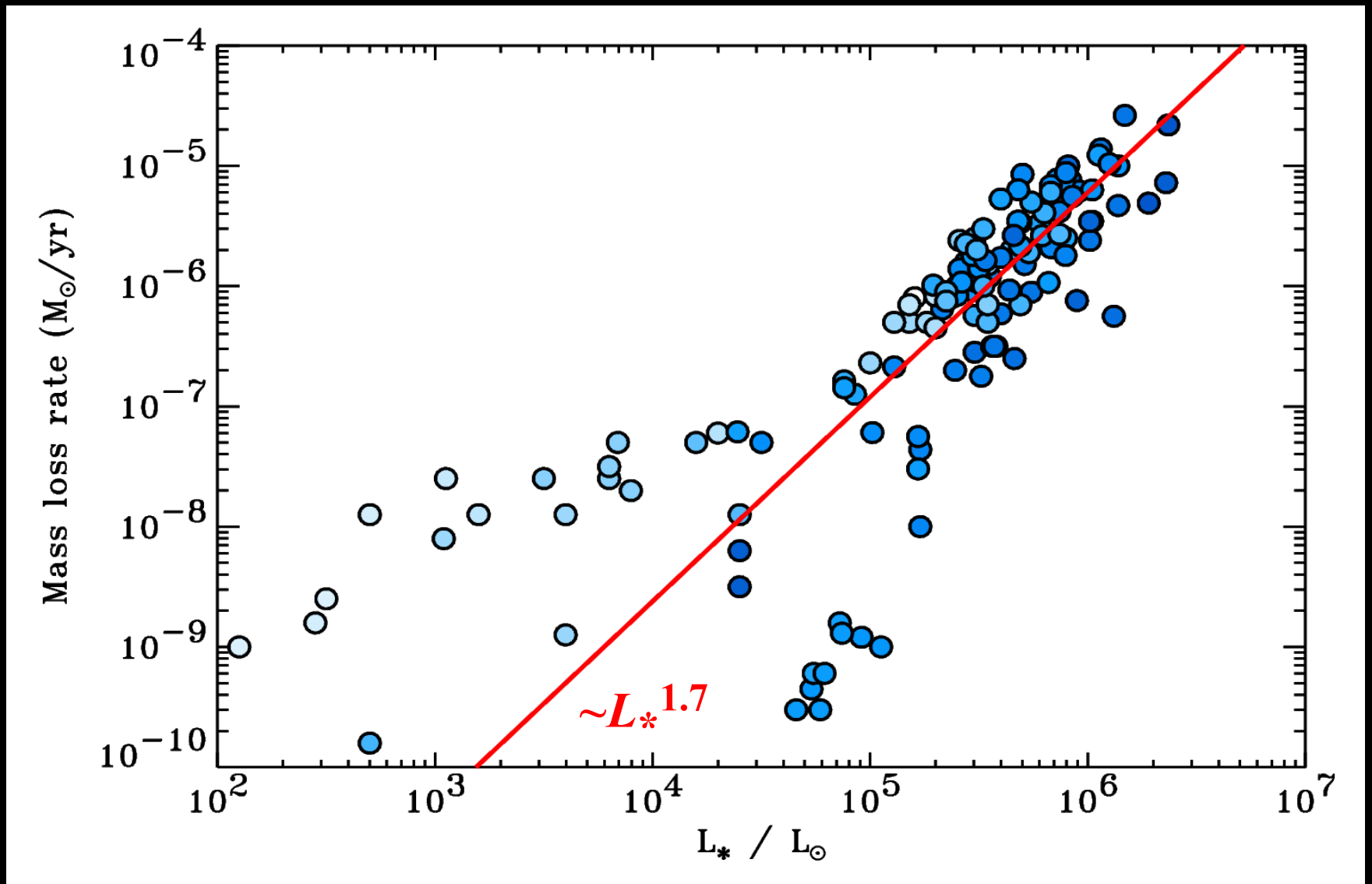
- Gravity must be counteracted above the photosphere (*not below*) by some continuously operating outward force . . .
 - **Gas pressure:** needs $T \sim 10^6$ K (“coronal heating”)
 - **Radiation pressure:** possibly important when $L_* > 100 L_\odot$
 - free electron (Thomson) opacity? (goes as $1/r^2$; needs to be supplemented)
 - ion opacity? ($T_{\text{eff}} \gtrsim 15,000$ K)
 - dust opacity? ($T_{\text{eff}} \lesssim 3,500$ K)
 - **Wave pressure / Shocks:** can produce time-averaged net acceleration
 - **MHD effects:** closed fields can be ejected (CMEs), or “plasmoids” can be pinched like melon seeds and carry along some of the surrounding material.



Stellar winds across the H-R Diagram

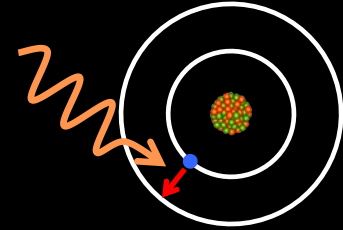


Massive star winds: observations



Massive star winds: radiative driving

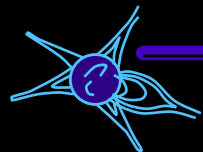
- Castor, Abbott, & Klein (1975) worked out how a hot star's radiation field can accelerate a time-steady wind, even if its "Eddington factor" $\Gamma \ll 1$.



$$\mathbf{a}_{\text{rad}} = \int d\nu \frac{\kappa_{\nu} \mathbf{F}_{\nu}}{c}$$

$$\Gamma = \frac{|\mathbf{a}_{\text{rad, thin}}|}{g} \approx 3 \times 10^{-5} \left(\frac{L_*/L_{\odot}}{M_*/M_{\odot}} \right)$$

- Bound electron resonances have higher cross-sections than free electrons (i.e., **spectral lines** dominate the opacity κ_{ν})
- In the accelerating wind, these narrow opacity sources become **Doppler shifted** with respect to the star's photospheric spectrum.
- Acceleration thus depends on velocity & velocity gradient! This turns " $F=ma$ " on its head! (Nonlinear feedback...)

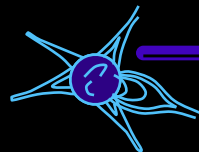
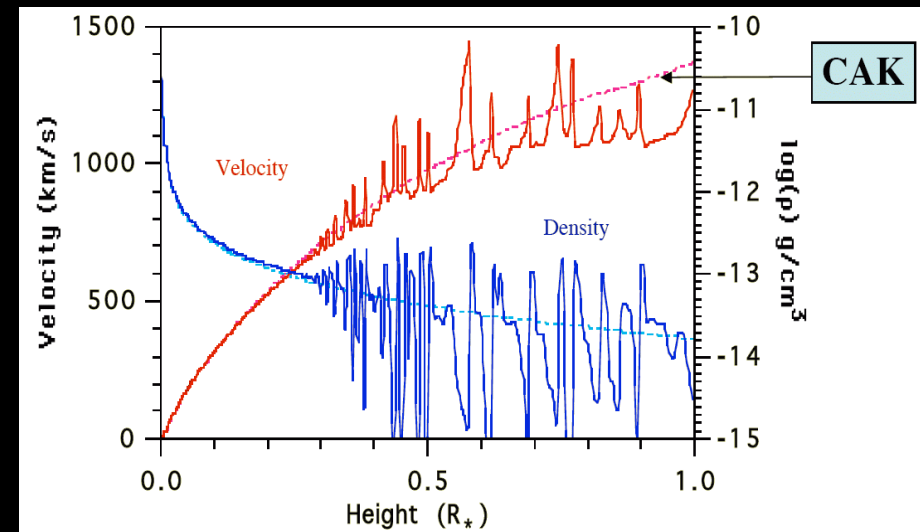


Massive star winds: radiative driving

- The Castor, Abbott, & Klein (CAK) theory gives a prediction for mass loss rates:

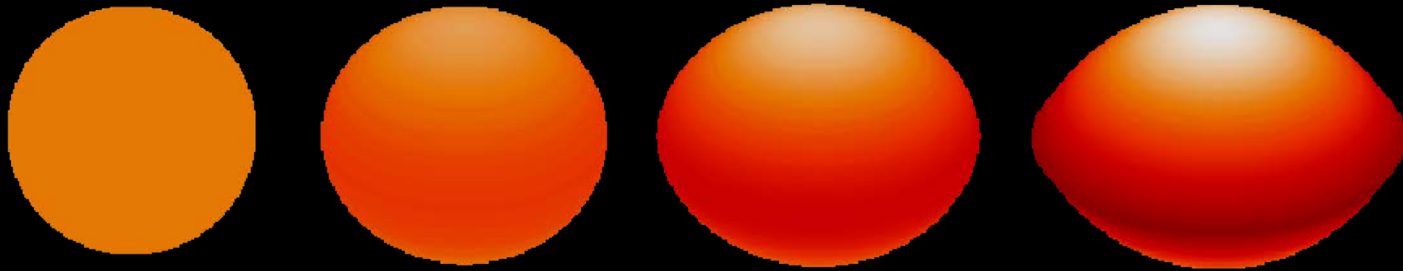
$$\begin{aligned}\dot{M}_{\text{CAK}} &\propto M_* \Gamma^{1.7} (1 - \Gamma)^{-0.7} (Z/Z_\odot)^{0.7} f(T_{\text{eff}}) \\ &\propto L_*^{1.7} M_*^{-0.7} (Z/Z_\odot)^{0.7} \quad (\Gamma \ll 1)\end{aligned}$$

- Metallicity dependence (largely) verified by observations in SMC and LMC, but it flattens out for lower Z (Vink 2008).
- “Clumping” can affect predicted mass loss rates by up to a factor of 10.
- What causes clumping? Radiative driving is **unstable!**



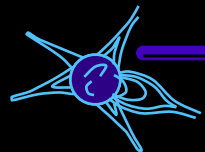
Rapid rotation

- Because of competition between gravity and centrifugal forces at the equator, rapid rotators become **oblate** and “gravity darkened” (von Zeipel 1924).

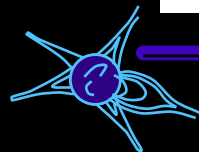
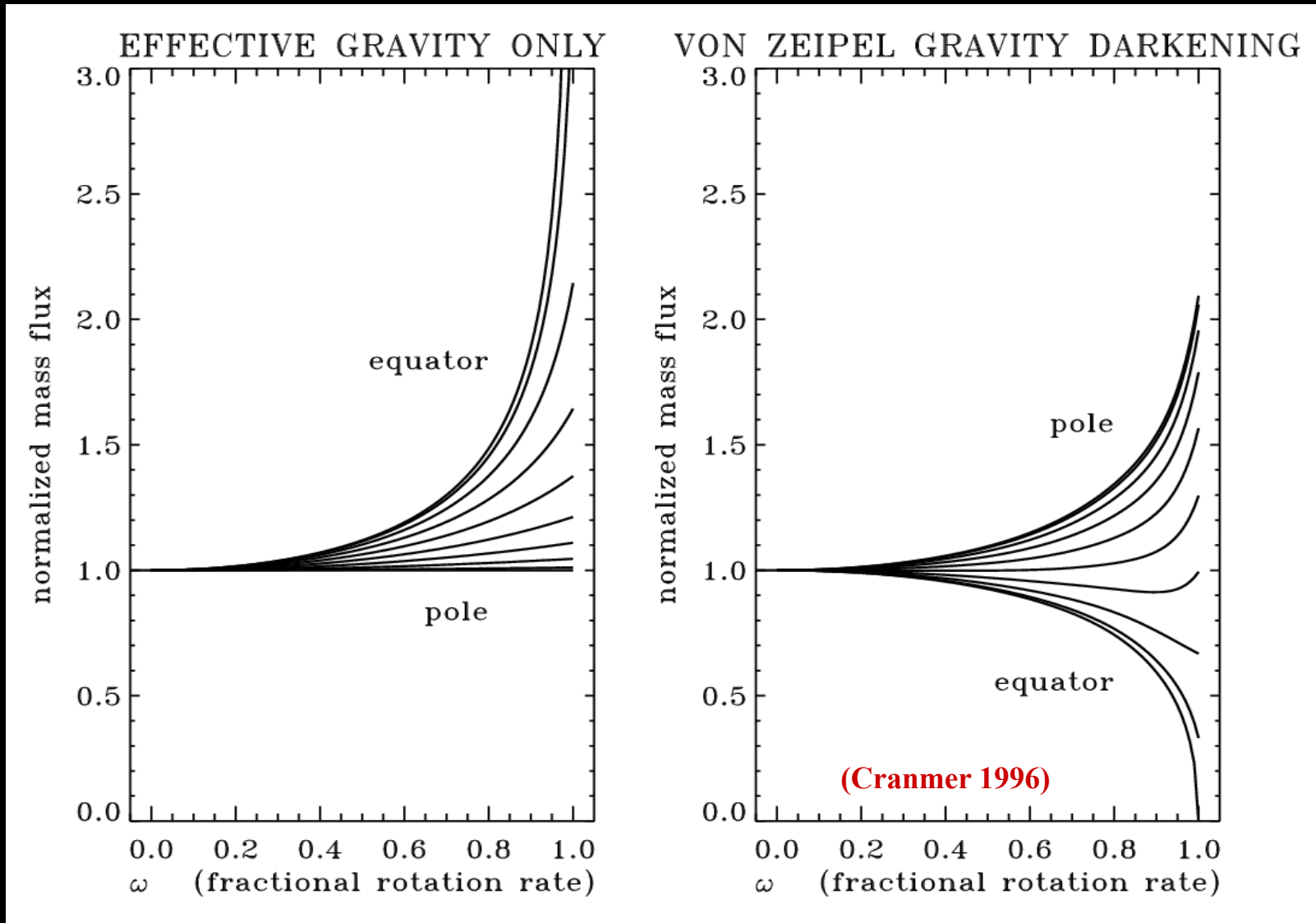


$$|\mathbf{F}_{\text{rad}}(\theta)| = \sigma T_{\text{eff}}^4(\theta) = L_* g^{4\beta} \left[\oint g^{4\beta} dS \right]^{-1}$$

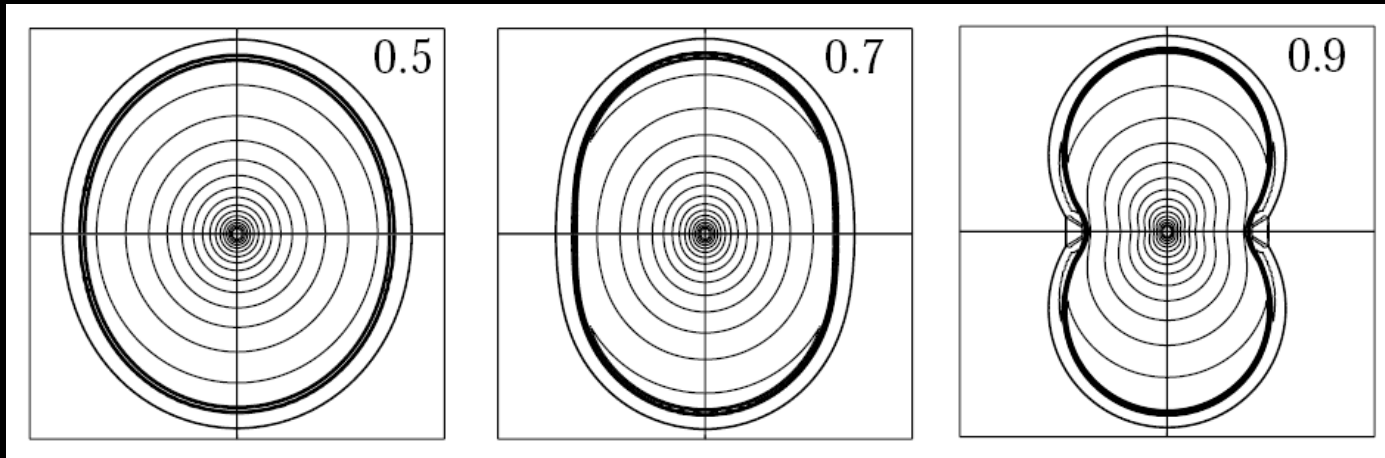
- Existence of gravity darkening has been confirmed via eclipsing binaries and visible interferometry of oblate stars.
- For hot stars with radiative interiors, $\beta \approx 0.25$ (down to late-A / early-F)
- For cooler stars with convective layers below photosphere, $\beta \approx 0$ to 0.08



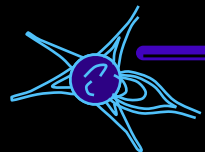
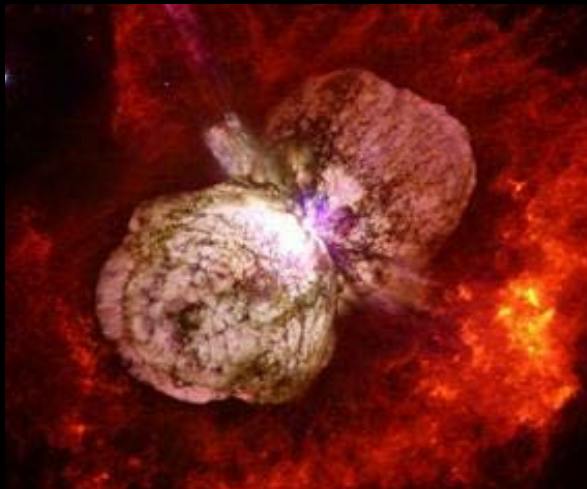
Rapid rotation: impact on mass loss



Rapid rotation: impact on mass loss

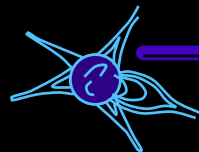
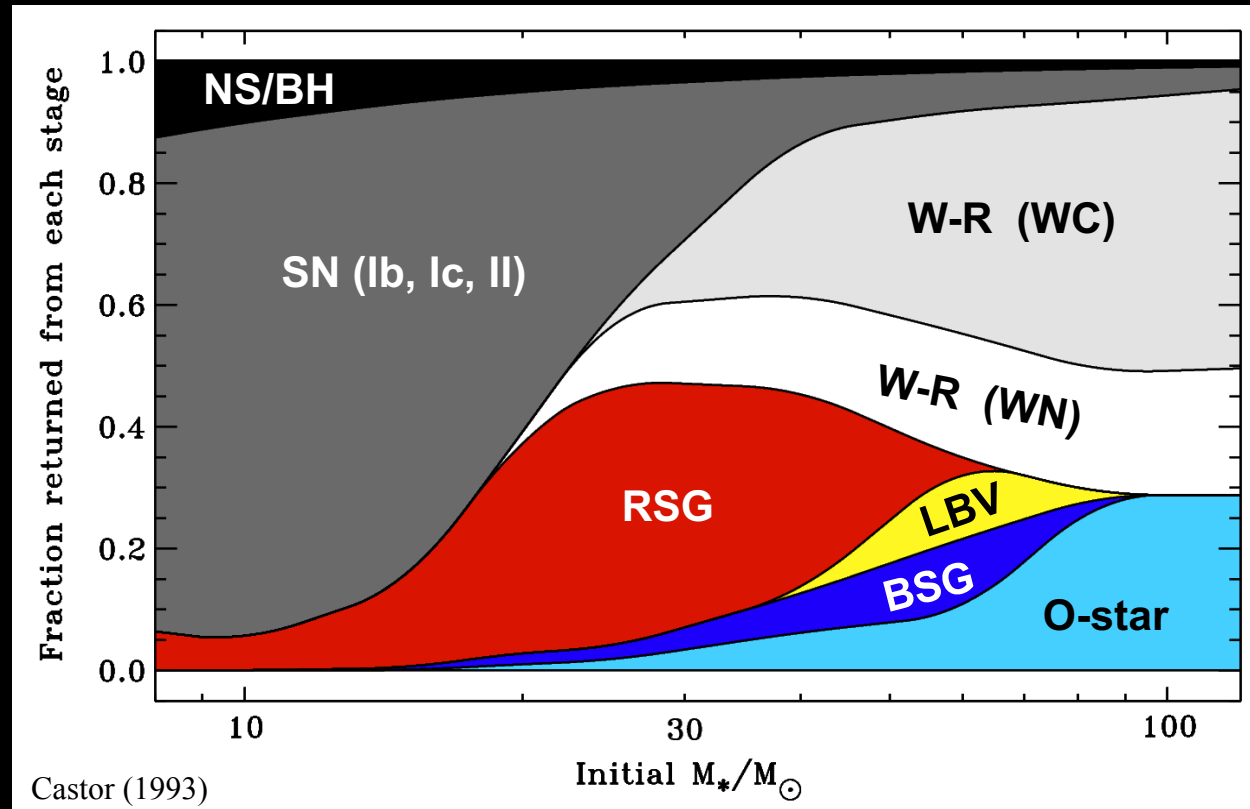


(Dwarkadas & Owocki 2002)



Massive star evolution: winds matter!

- Mass loss affects evolutionary tracks (isochrones, cluster HB/RGB), SN yields.
- Hot-star winds influence ISM abundances & ionization state of Galaxy.
- **Wolf-Rayet stars:** H stripped off by O-star wind; dense, multiple-scattering CAK.

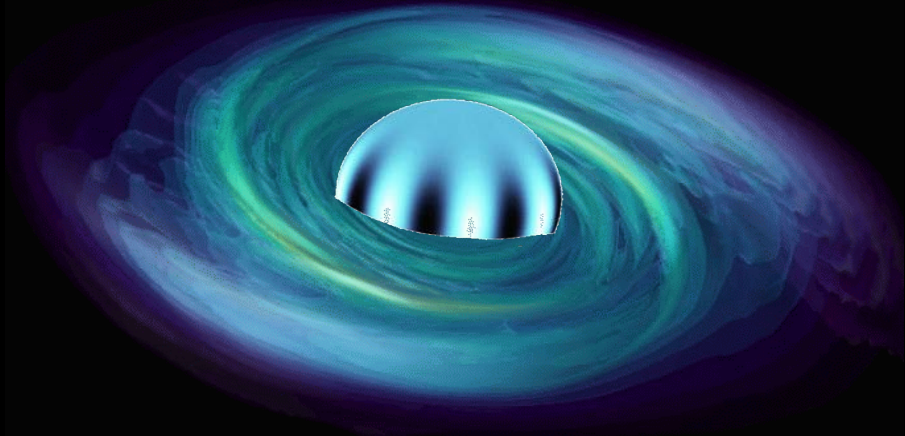


Be stars: “decretion disks”

- **Classical Be stars** are non-supergiant B stars with emission in H Balmer lines.
- Be stars are rapid rotators, but are *not* rotating at “critical” / “breakup:”

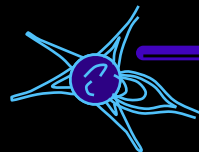
$$V_{\text{rot}} \approx (0.5 \text{ to } 0.9) V_{\text{crit}}$$

- How does angular momentum get added to the circumstellar gas?

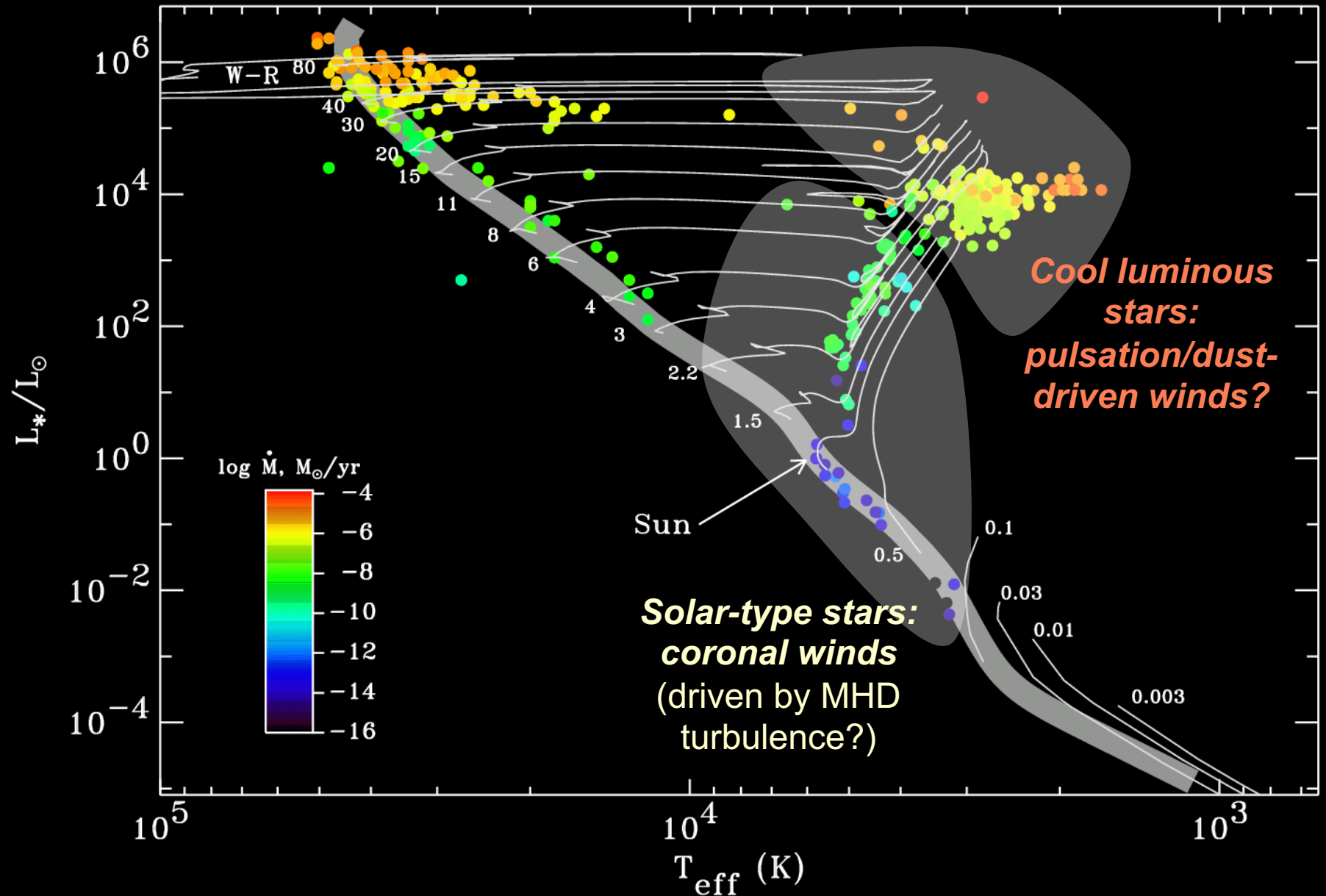


Hints:

- Many (all?) Be stars undergo nonradial pulsations (NRPs).
- Rivinius et al. (1998, 2001) found correlations between emission-line “outbursts” and constructive interference (“beating”) between NRP periods.
- Ando (1986) & Saio (1994) suggested that NRPs can transfer angular momentum outwards. More detailed models show that this *can* provide enough “**spinup**” for centrifugal forces to cancel gravity (Cranmer 2009).



Stellar winds across the H-R Diagram



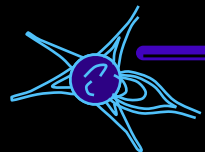
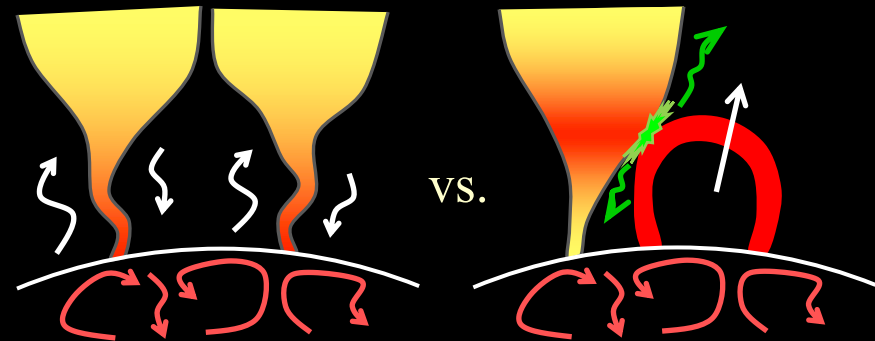
The solar wind

- **Parker (1958)** proposed that gas pressure in the hot ($T > 10^6$ K) corona counteracts gravity and accelerates a steady supersonic wind. **1962:** *Mariner 2* confirmed it.



Decades of remote sensing & *in situ* probing have revealed much of the physics of this turbulent MHD system . . .

- What determines how much energy and momentum goes into the solar wind?
 - Waves & turbulence input from below?
 - Reconnection & mass input from loops?

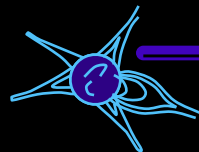
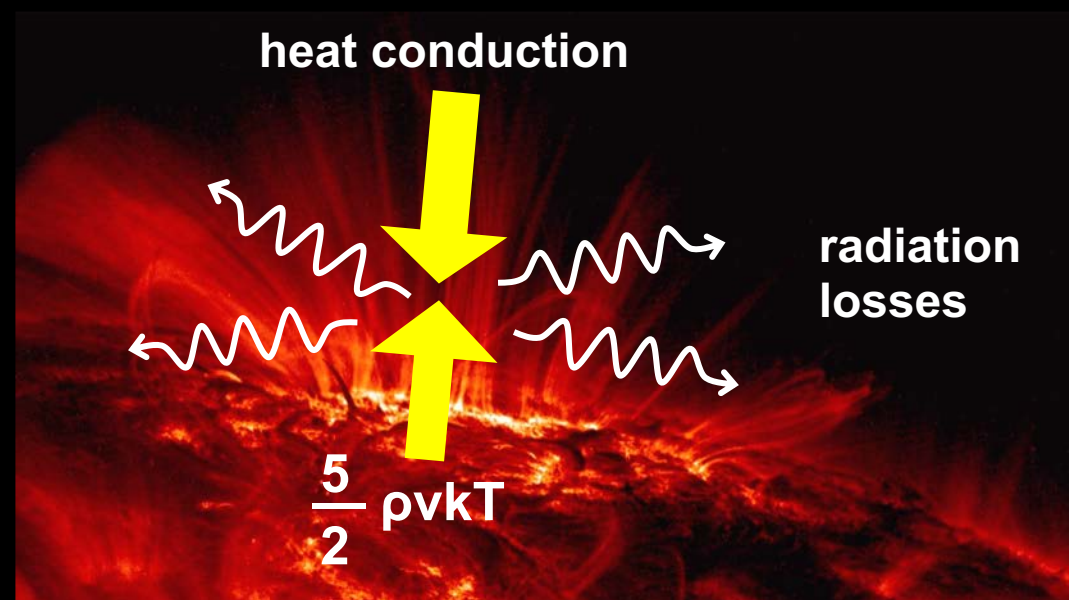
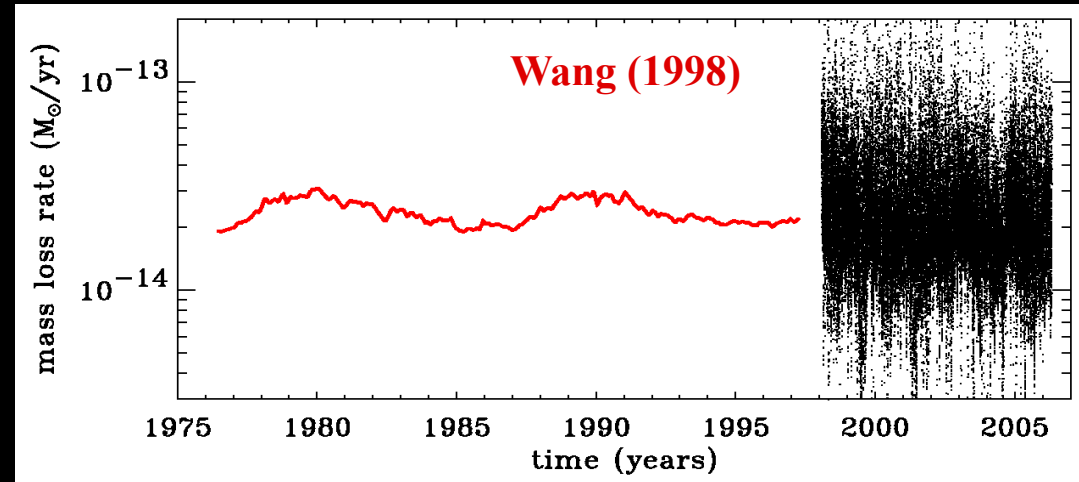


What sets the Sun's mass loss?

- The sphere-averaged mass flux is remarkably constant.
- Coronal heating seems to be ultimately responsible, but that **varies by orders of magnitude** over the solar cycle.
- Hammer (1982) & Withbroe (1988) suggested an energy balance with a “thermostat.”
- Only a fraction of total coronal heat flux conducts down, but in general, we expect something close to

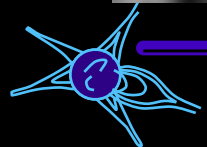
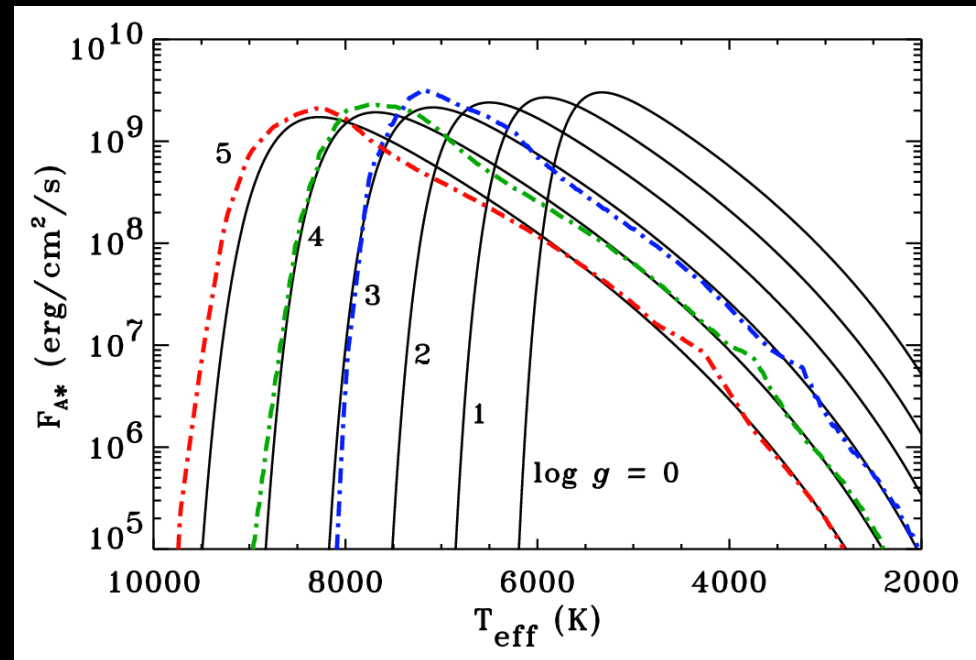
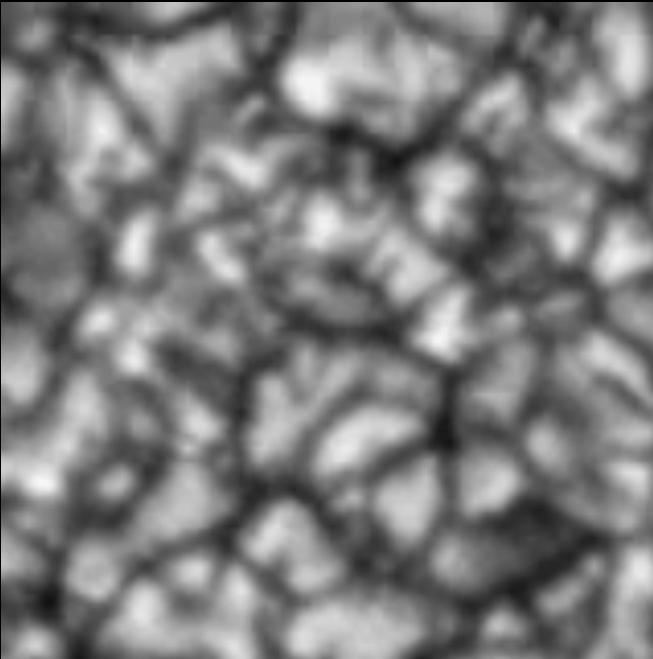
$$\dot{M} \propto F_{\text{heat}} \propto F_X$$

... along open flux tubes!

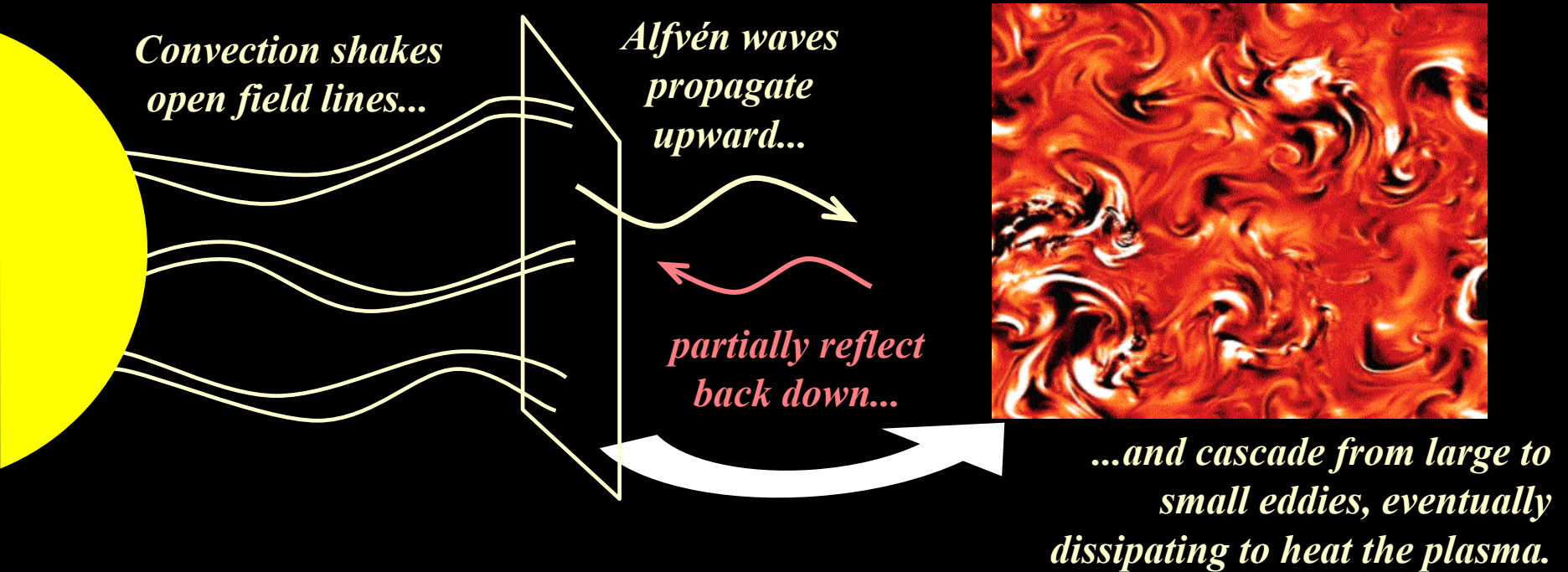


Convection-driven MHD waves

- Cranmer & Saar (2011) focused on Alfvén waves as primary source of heating.
- Other sources of energy & momentum probably exist, but we chose to explore how much can be explained with just this one set of processes.
- Turbulent convection excites waves (Lighthill 1952), and in a magnetized stellar atmosphere the dominant type of waves should be transverse “kink modes” (Musielak & Ulmschneider 2002).

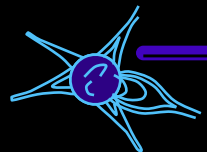


Heating from MHD turbulence



- MHD simulations inspire “phenomenological” scalings:

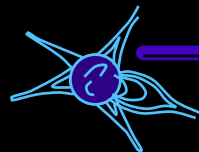
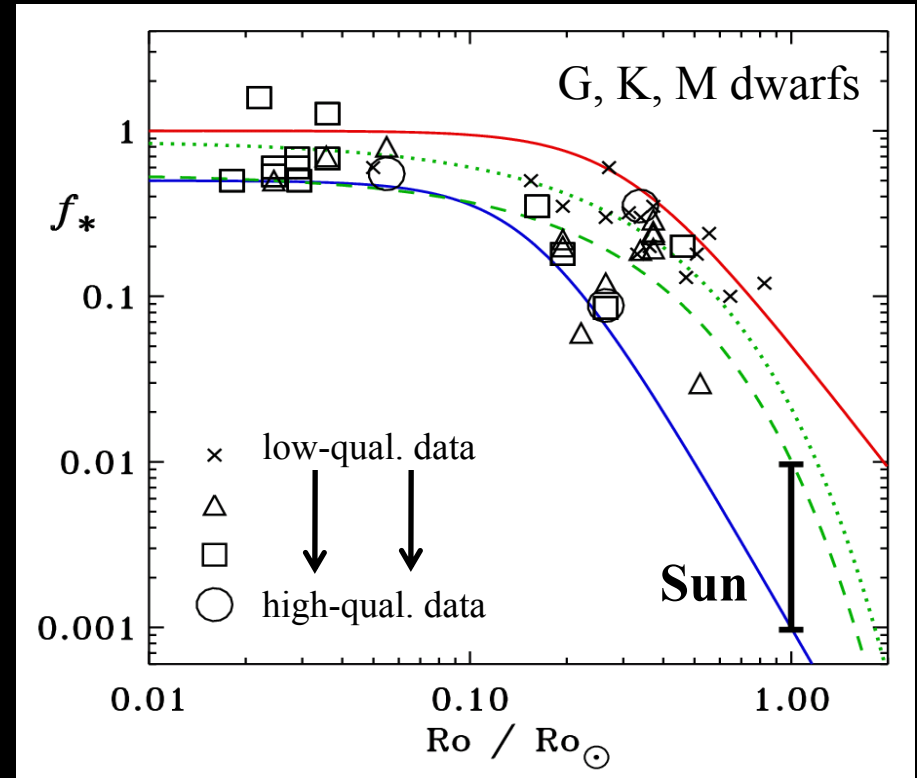
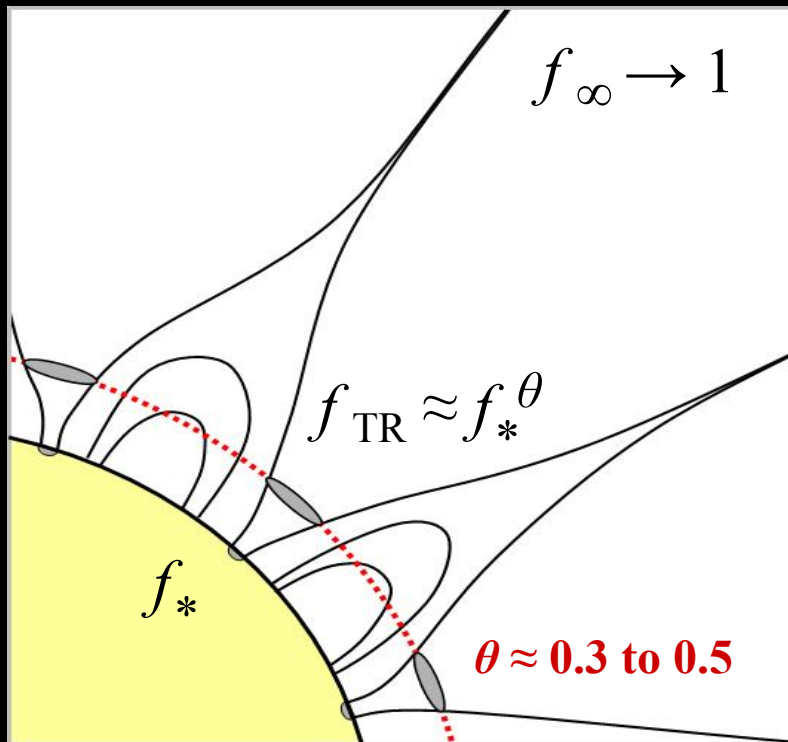
$$Q_{\text{heat}} = |\nabla \cdot \mathbf{F}_{\text{heat}}| \approx \frac{\rho v^3}{\ell} \approx \frac{\varepsilon \rho (v_+^2 v_- + v_-^2 v_+)}{4\ell_{\perp}}$$



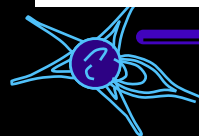
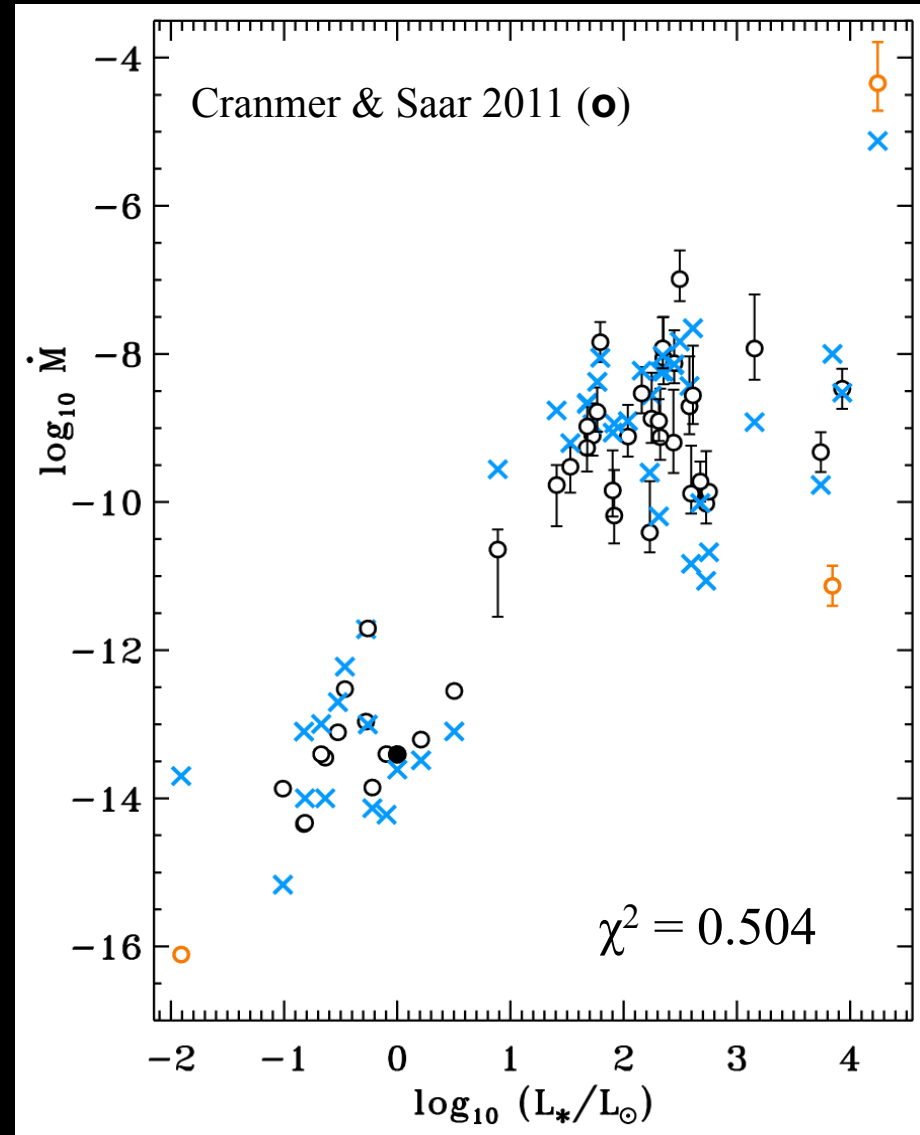
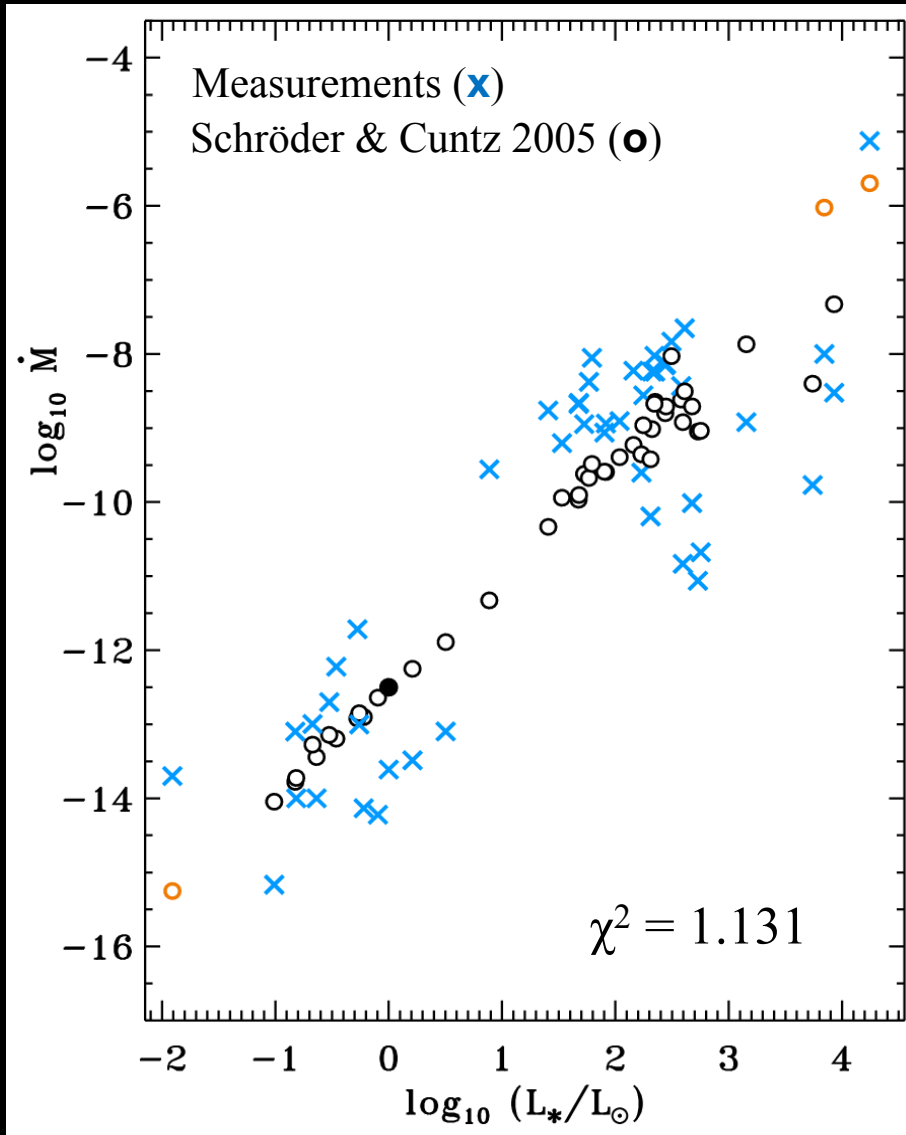
Open magnetic flux tubes

- The evolution of Q_{heat} with height depends on the magnetic field . . .
- Mass flux depends on the area covered by **open** field lines at the TR:

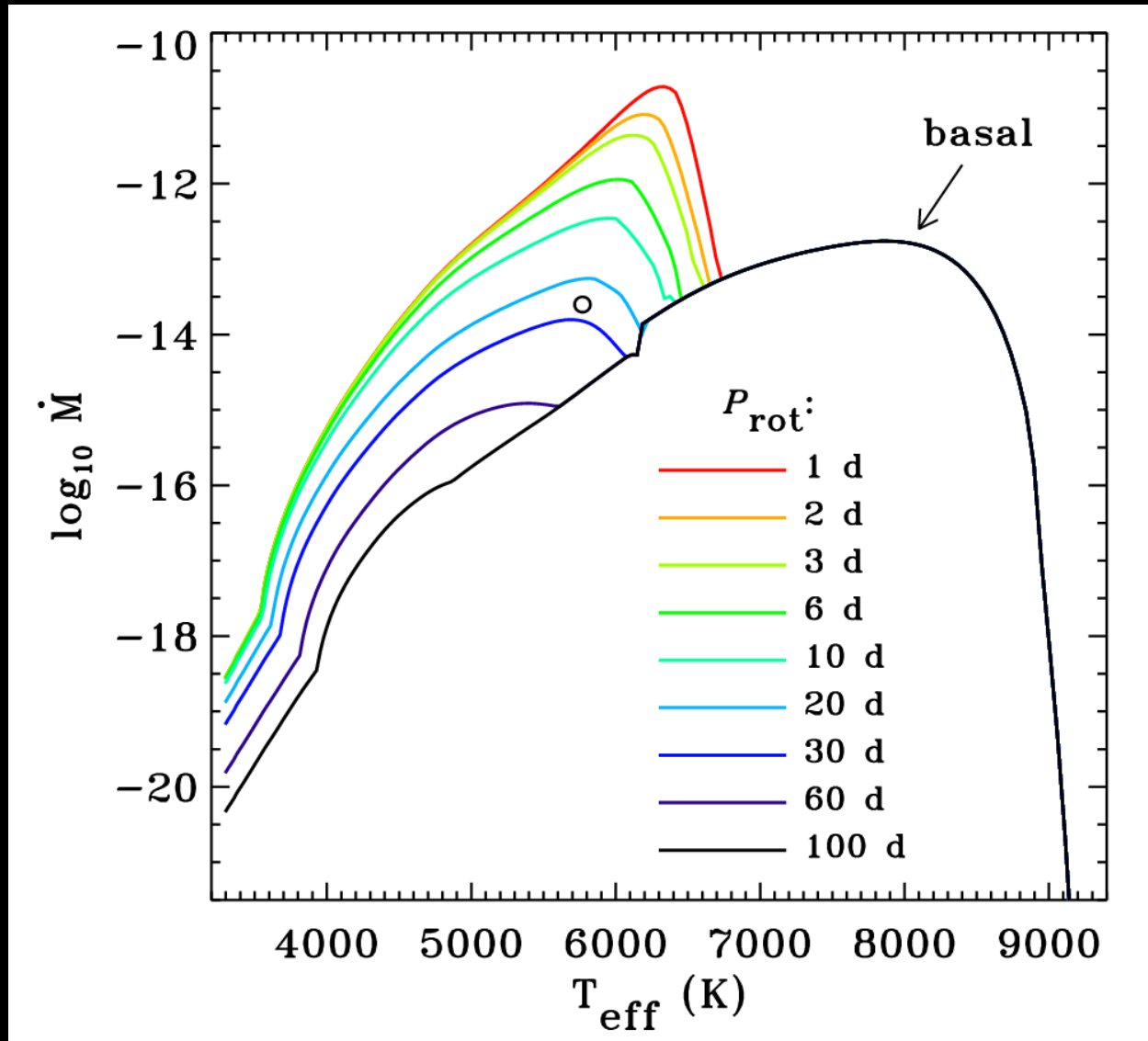
$$A = 4\pi r^2 f$$
- Measurements of Zeeman-broadened lines constrain the filling factor of (open + closed) photospheric B-field.



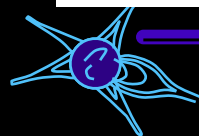
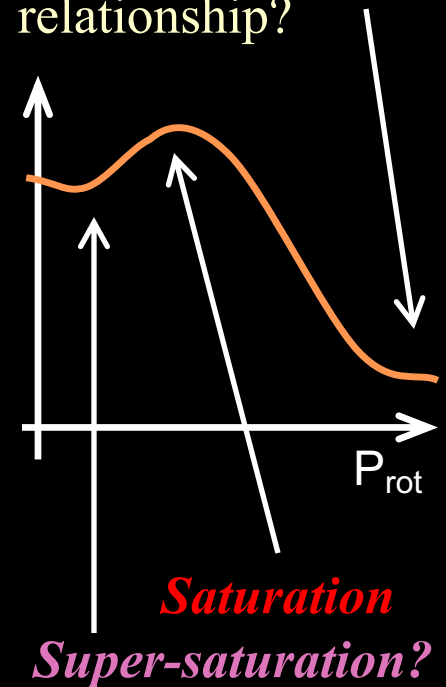
Results for 47 cool stars with measured \dot{M}



Mass loss on an ideal main sequence

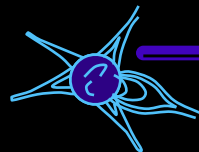
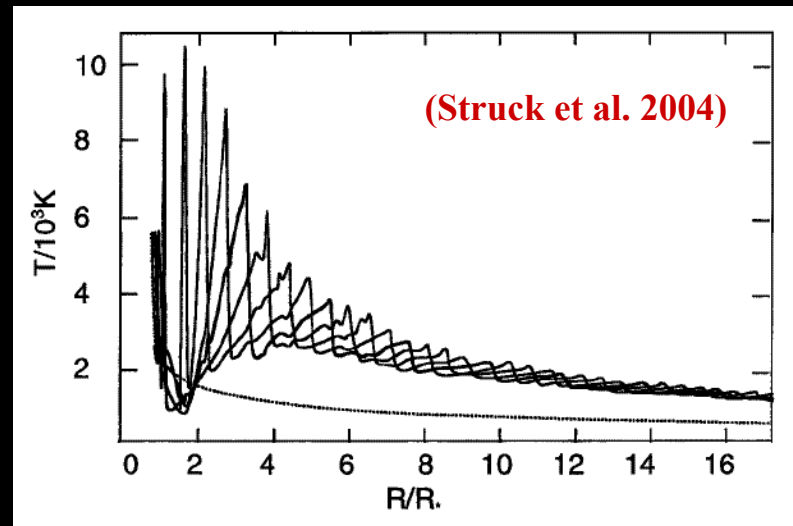
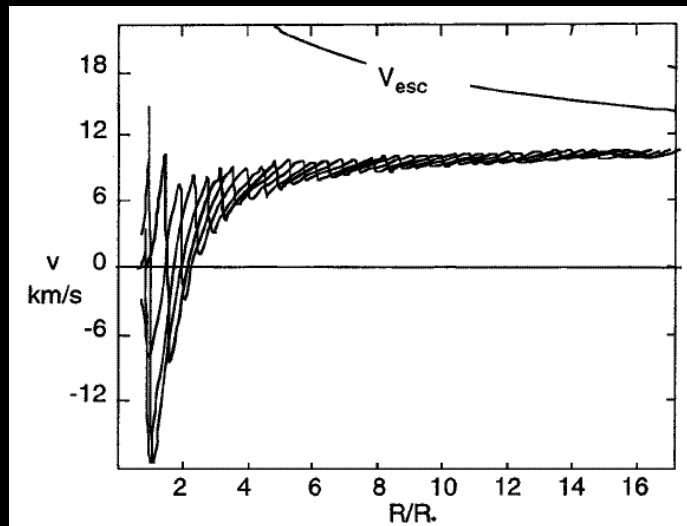
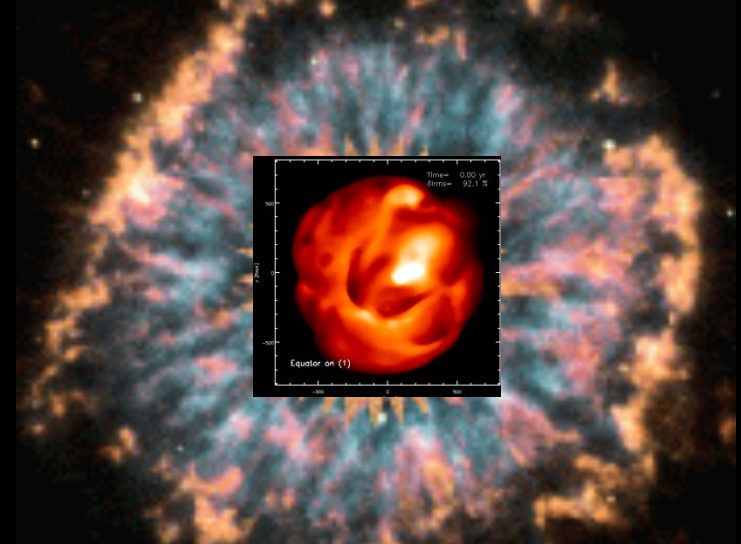


- Is there really a basal “floor” in the age-rotation-activity relationship?



Evolved cool stars: RG, HB, AGB, Mira

- The extended atmospheres of red giants and supergiants are likely to be **cool** (i.e., not highly ionized or “coronal” like the Sun).
- High-luminosity: radiative driving... of dust?
- Shock-heated “**calorispheres**” (Willson 2000) ?
- Numerical models show that pulsations couple with radiation/dust formation to be able to drive mass loss rates up to 10^{-5} to $10^{-4} M_{\odot}/\text{yr}$.



Radio diagnostics of winds/coronae: Future prospects?

Multi-thermal atmospheres:

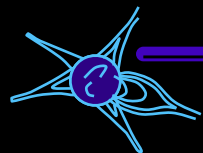
- *Cool luminous stars*: UV spectroscopy detects “warm” chromospheric gas. Radio & IR detect “cold” dust-forming gas. Do these outflowing populations **coexist?**

Age-Rotation-Activity relations:

- Can combined radio & X-ray data help answer questions about “super-saturation” or the “basal flux floor?”

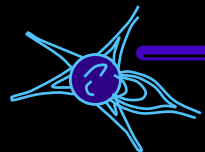
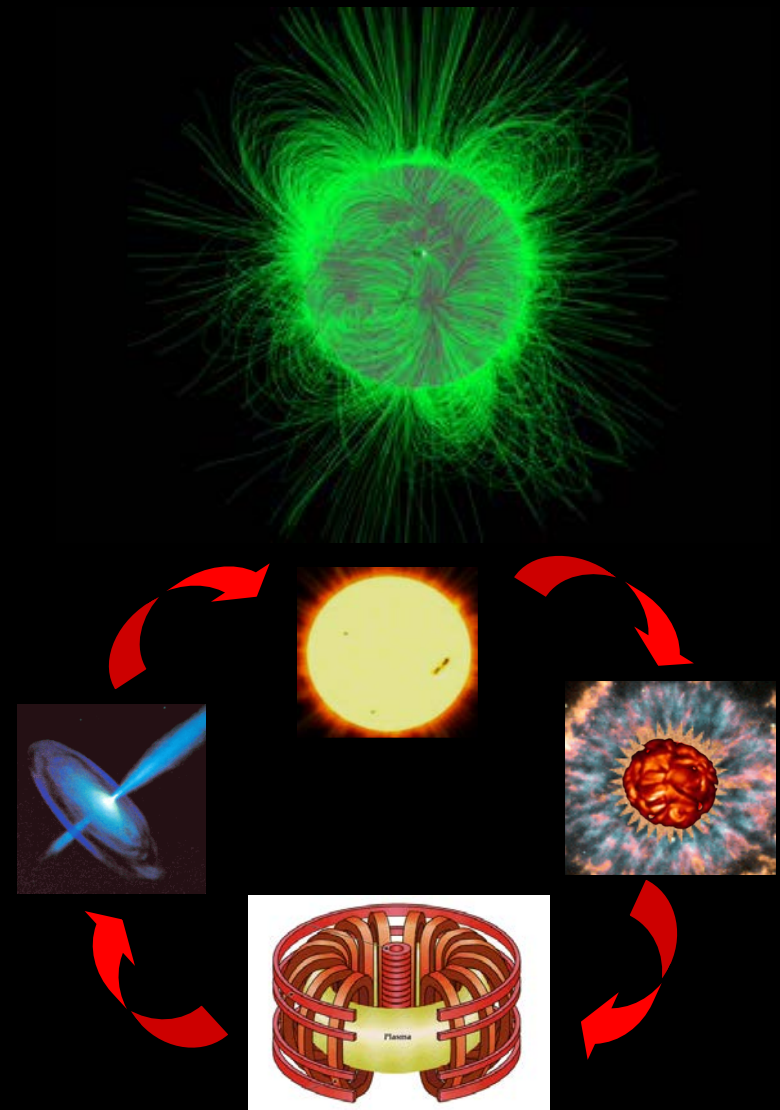
Magnetic fields:

- Can combined radio (gyroresonance emission) & optical (Zeeman-broadened line) data better constrain weak-field ($B < 50$ G) “**filling factors?**”
- *Massive stars*: There are many new measurements of B-fields (MiMeS project). Is **nonthermal/synchrotron** radio emission preferentially strong in these stars, or does the traditional (?) interpretation of “wind shocks” hold up?

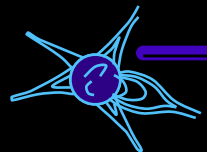


Conclusions

- Within an order of magnitude, theories aren't doing *too* badly in predicting mass loss rates... but to get a decent estimate, **lots of information** about the star is needed (e.g., luminosity, mass, age, rotation period, magnetic field, pulsational properties).
- Simulations of **stellar interiors** are still the key to unlocking many puzzles, since the properties of rotation, pulsation, convection, dynamos, etc., are all determined “down there.”
- Understanding is greatly aided by ongoing collaboration between the solar physics, plasma physics, and astrophysics communities.

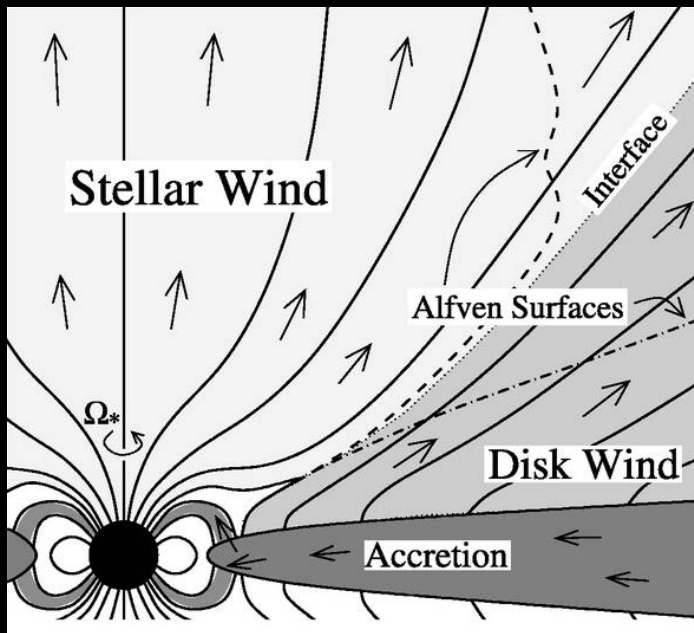


Extra slides . . .

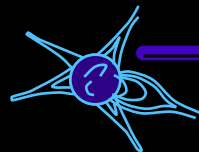
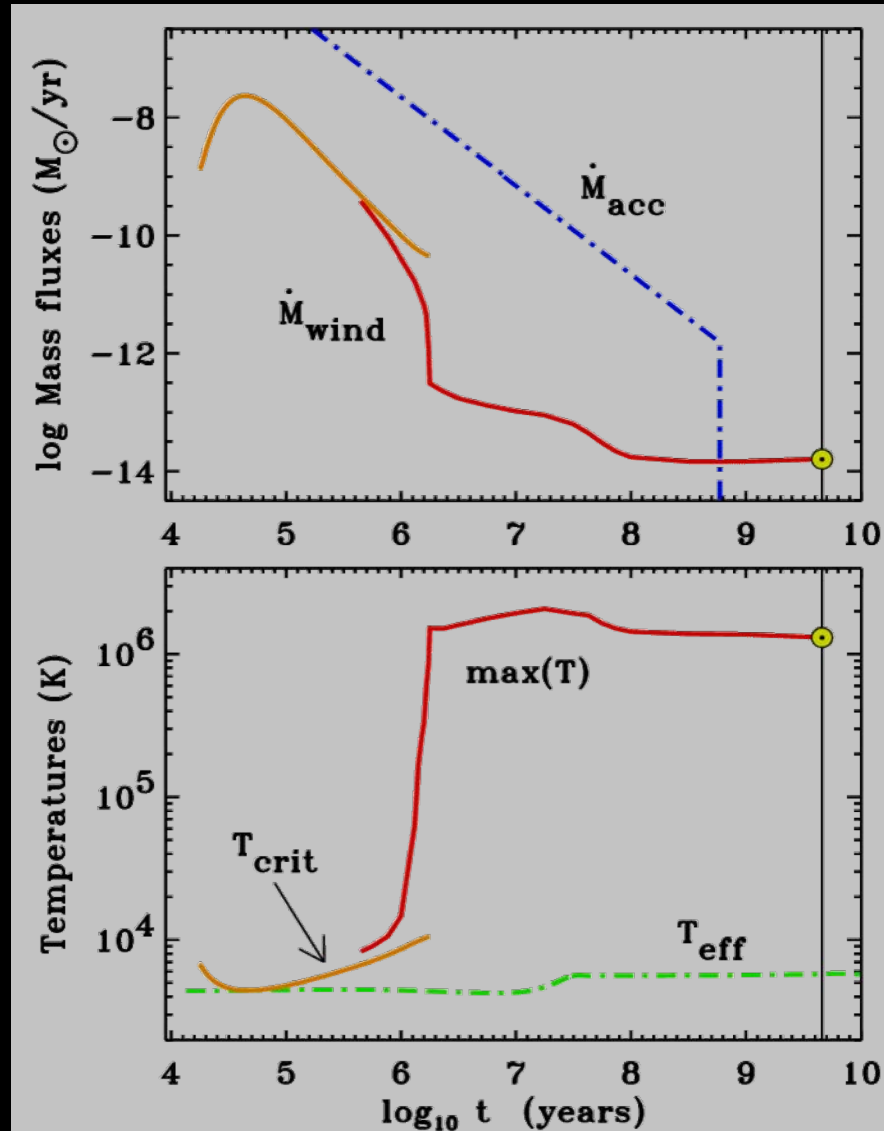


Young cool stars: classical T Tauri

- T Tauri stars exhibit disks, magnetospheric accretion streams, X-ray coronae, and various kinds of polar outflow.
- Cranmer (2008, 2009) modeled coronal heating & mass loss via **turbulence** excited on the surface by accretion impacts.

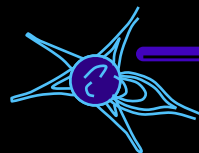
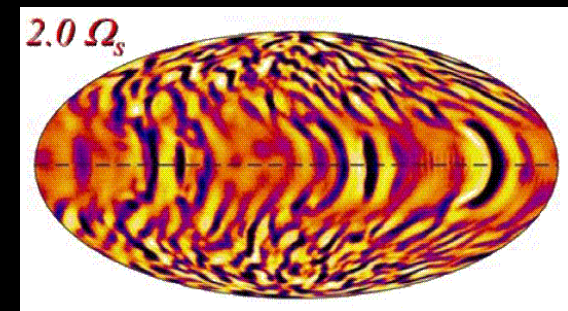
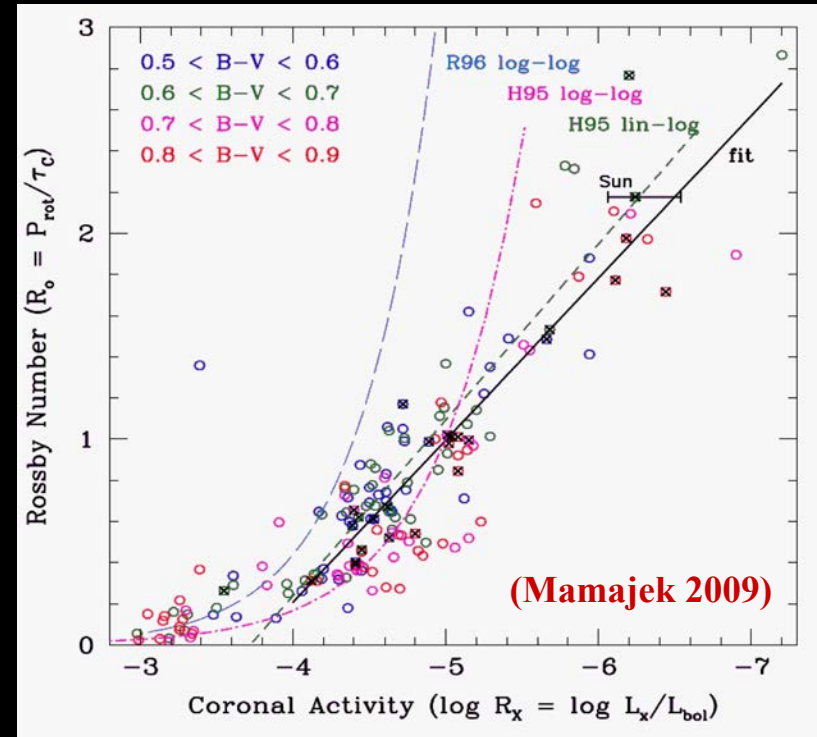


(Matt & Pudritz 2005, 2008)



Cool-star rotation \rightarrow mass loss?

- There is a well-known “rotation-age-activity” relationship that shows how coronal heating weakens as young (solar-type) stars age and spin down (Noyes et al. 1984).
- X-ray fluxes also scale with mean magnetic fields of dwarf stars (Saar 2001).
- For solar-type stars, mass loss rates scale with coronal heating & field strength.
- What’s the cause? With more rapid rotation,
 - **Convection** may get more vigorous (Brown et al. 2008, 2010) ?
 - Lower effective gravity allows more magnetic flux to emerge, thus giving a higher **filling factor** of flux tubes on the surface (Holzwarth 2007)?



Cool-star dimensional analysis . . .

- Stellar wind power:

$$L_{\text{wind}} = \dot{M} \left(V_{\text{esc}}^2 + v_{\infty}^2 + \left\{ \begin{array}{l} \text{heat?} \\ \text{waves?} \end{array} \right\} \right) \sim \frac{GM_* \dot{M}}{R_*}$$

- Reimers (1975, 1977) proposed a semi-empirical scaling:

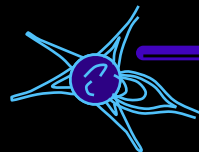
$$L_{\text{wind}}/L_* \sim \text{constant} \quad \longrightarrow \quad \dot{M} \propto L_* R_* / M_*$$

- Schröder & Cuntz (2005) investigated an explanation via **convective turbulence** generating atmospheric waves . . .


$$L_{\text{wind}} = 4\pi R_*^2 F_{\text{mech}} \propto (L_*/T_{\text{eff}}^4) T_{\text{eff}}^p \quad (p \approx 6 \text{ to } 10)$$

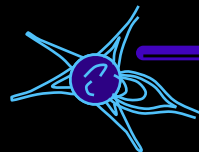
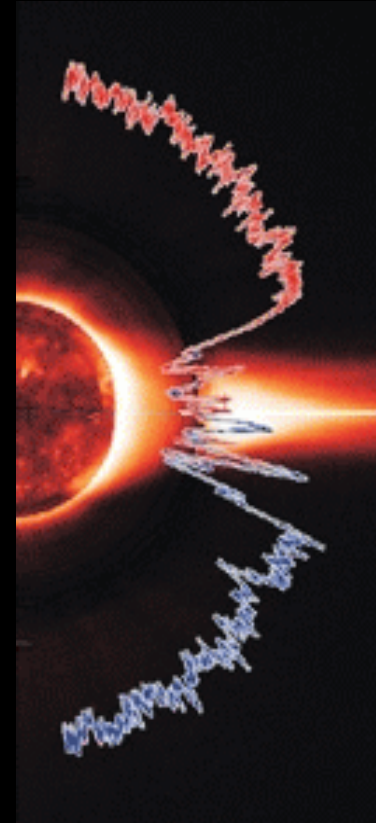
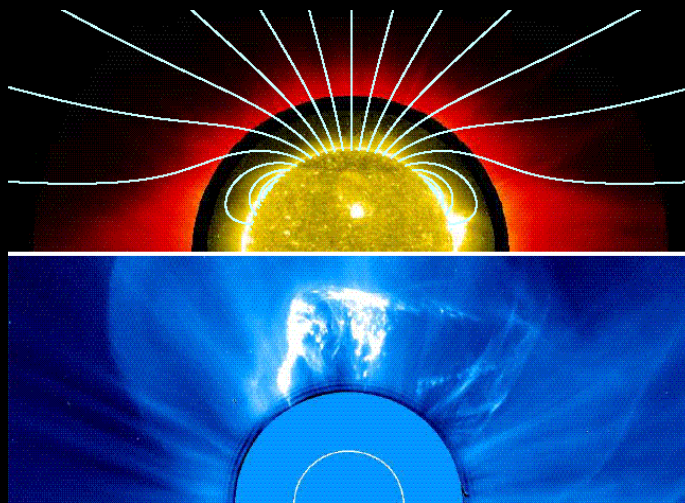
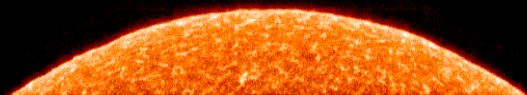
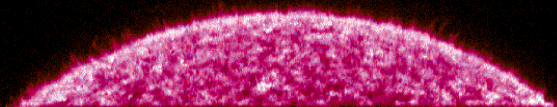
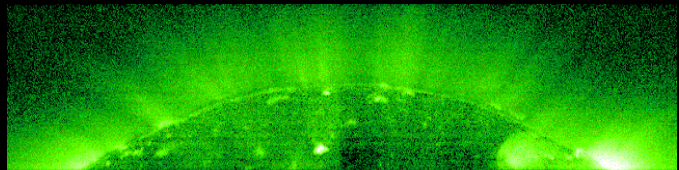
$$\dot{M} \propto L_* R_* T_{\text{eff}}^{p-4} / M_*$$

- Use caution with “ p ” exponent: once $T_{\text{eff}} > 7000 \text{ K}$, it flattens out ($p \rightarrow 0$).
- For $T_{\text{eff}} > 9000 \text{ K}$, F_{mech} plummets because convection zone disappears!



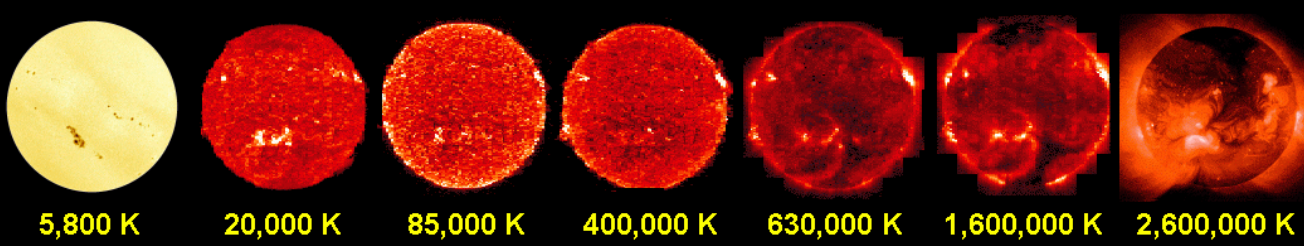
The solar wind: very brief history

- **Mariner 2** (1962): first direct confirmation of continuous supersonic solar wind, validating Parker's (1958) model of a gas-pressure driven wind.
- **Helios** probed in to 0.3 AU, **Voyager** continues past 100+ AU.
- **Ulysses** (1990s) left the ecliptic; provided 3D view of the wind's connection to the Sun's magnetic geometry. 
- **SOHO** gave us new views of "source regions" of solar wind and the physical processes that accelerate it . . .



The coronal heating problem

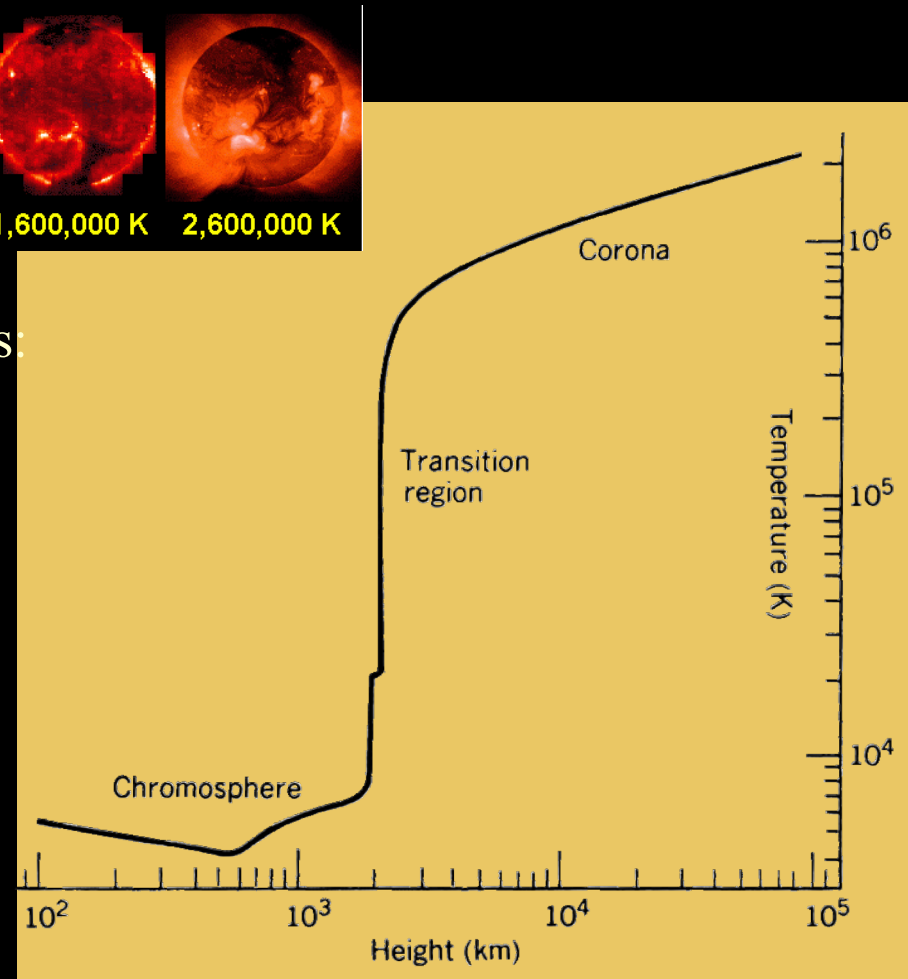
- We still don't understand the physical processes responsible for heating up the coronal plasma. A lot (not all!) of the heating occurs in a narrow "shell."



- Most suggested ideas involve 3 general steps:

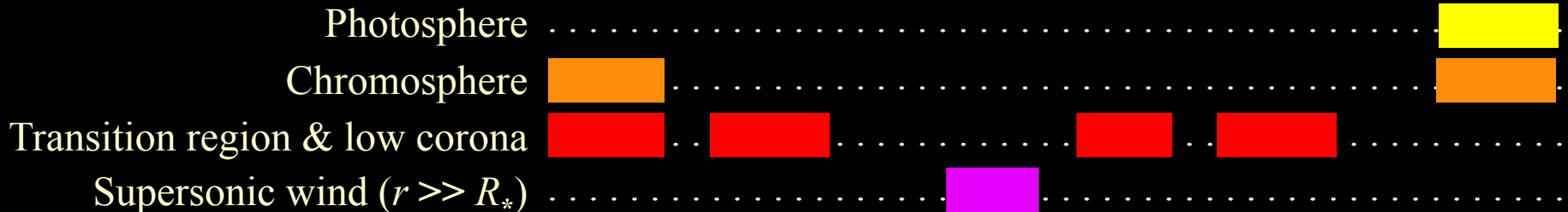
1. Churning convective motions that tangle up magnetic fields on the surface.
2. Energy is "stored" (above the photosphere) in the magnetic field.
3. Energy is released as heat, either via particle-particle or wave-particle "collisions."

Heating → Solar wind acceleration



Energy conservation in outer stellar atmospheres

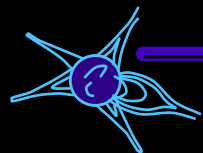
$$\frac{\partial}{\partial t} \left(\frac{\rho v^2}{2} + \frac{3P}{2} \right) + \nabla \cdot \left[\mathbf{F}_{\text{heat}} + \mathbf{F}_{\text{cond}} + \rho \mathbf{v} \left(\frac{v^2}{2} + \frac{5P}{2\rho} - \frac{GM_*}{r} \right) \right] = Q_{\text{rad}}$$



- Leer et al. (1982) and Hansteen et al. (1995) found that one can often simplify the energy balance to be able to solve for the mass flux:

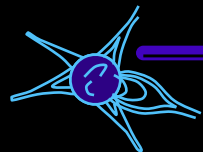
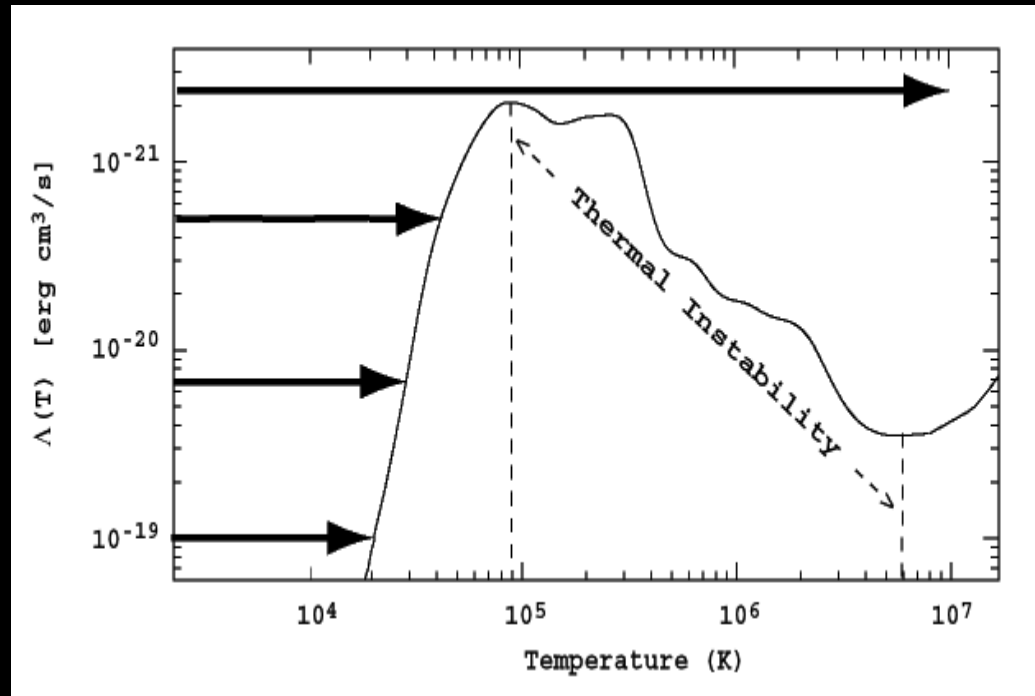
$$\left[A (F_{\text{heat}} - F_{\text{cond}}) - \dot{M} \frac{GM_*}{r} \right]_{\text{TR}} \approx \left[\dot{M} \frac{v^2}{2} \right]_{\infty}$$

- However, the challenge is to determine values for all the parameters!



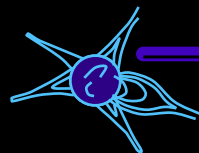
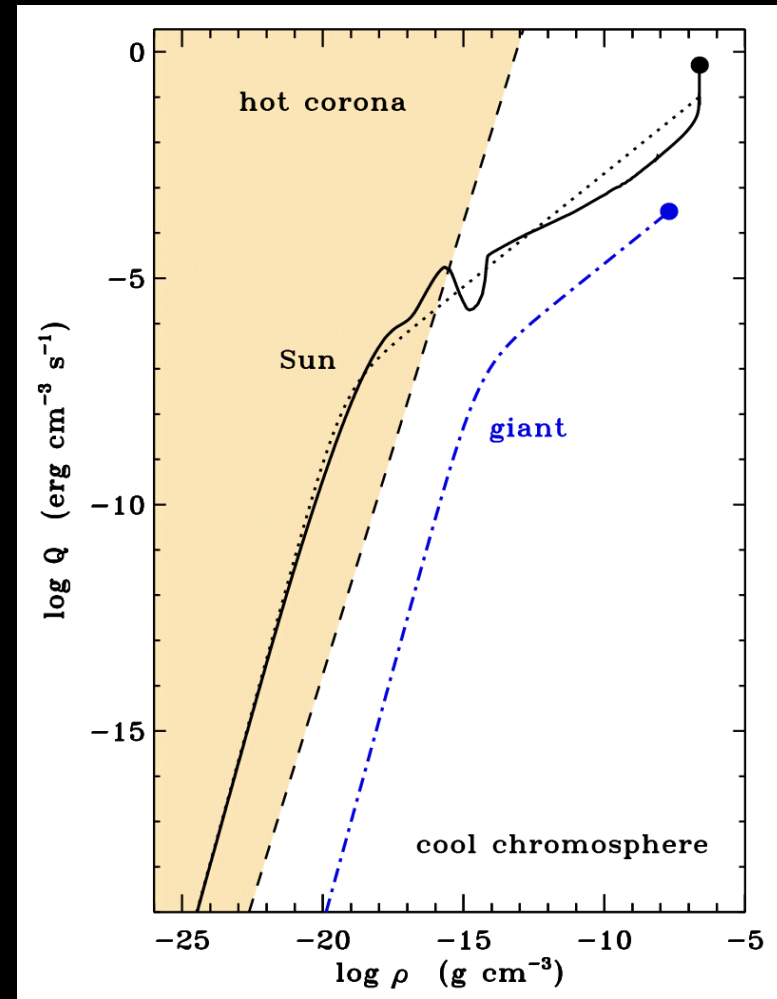
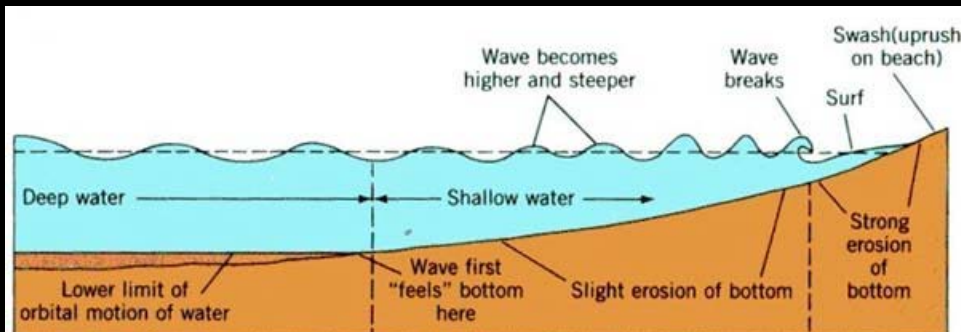
How can massive winds be “cold?”

- The extended solar corona is so low-density, the conservation of internal energy is essentially a balance between **local heating**, **downward conduction**, and **upward adiabatic losses**.
- When the outer atmosphere becomes massive enough, though, **radiative cooling** [$\sim \rho^2 \Lambda(T)$] becomes more efficient throughout the wind:
- The high-density wind becomes an **extended chromosphere** (supported by wave pressure??).
- For this case, Holzer et al. (1983) showed the energy equation is \sim irrelevant in determining mass flux! A simple analytic model (of the momentum equation) suffices.



Do Alfvén waves always heat a corona?

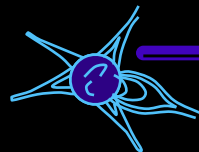
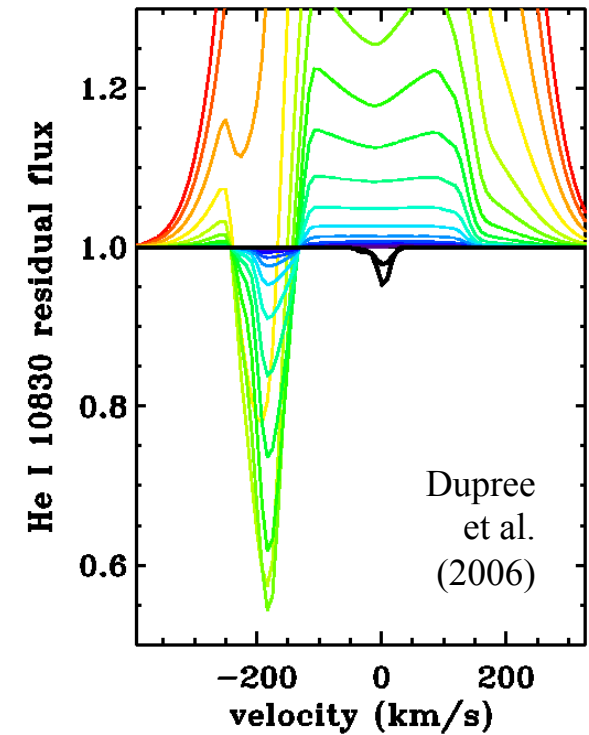
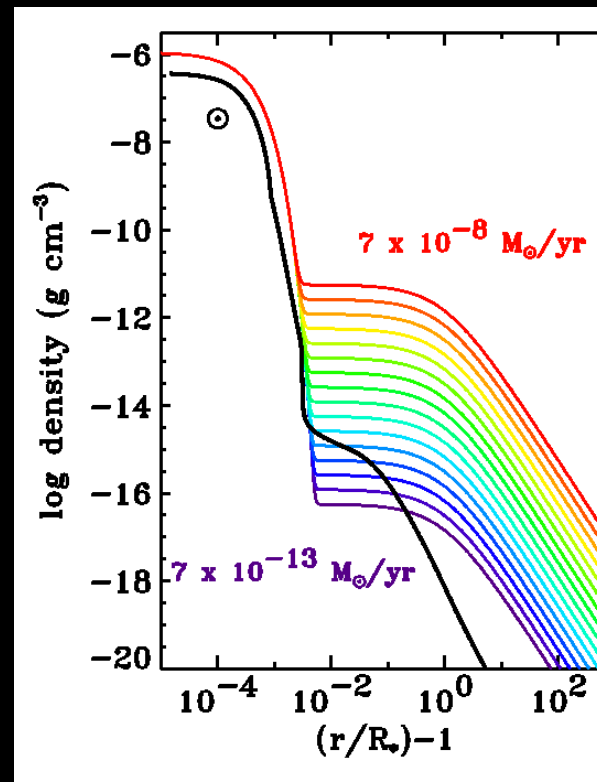
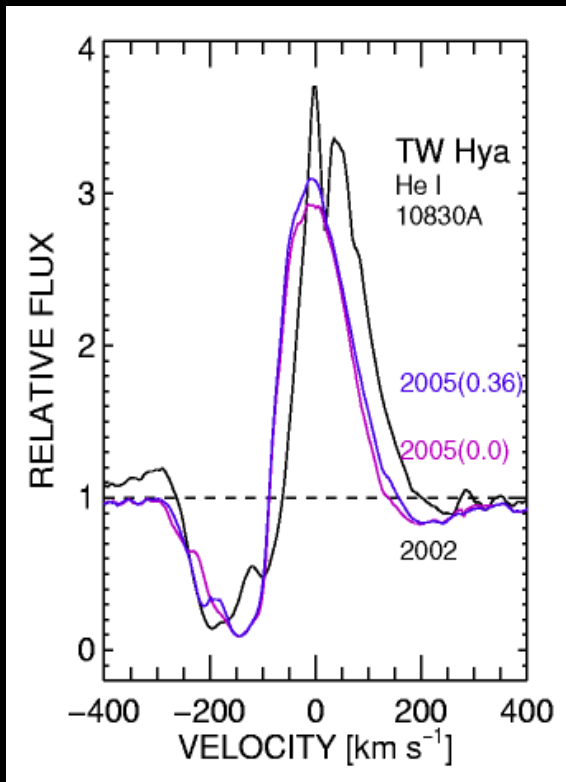
- With the above inputs (and assuming $v_\infty \approx V_{\text{esc}}$), we can solve for the mass loss rate in the case of a “hot coronal wind.”
- Sometimes, the heating rate Q drops off more steeply (with decreasing density ρ) than in the solar case, and radiative cooling always remains able to keep $T < 10^4$ K.
- In those “cold” cases (usually for luminous giants), gas pressure cannot accelerate a wind.
- Alfvén wave pressure may take the place of gas pressure (Holzer et al. 1983).



Multi-line spectroscopy

1990s: more self-consistent treatments of radiative transfer AND better data (GHRS, FUSE, high-spectral-res ground-based) led to better stellar wind diagnostic techniques!

A nice example: He I 10830 Å for TW Hya (pole-on T Tauri star) . . .



New ideas: astrosphere absorption

- Wood et al. (2001, 2002, 2005) distinguished cool ISM H I Ly α absorption from hotter “piled up” H 0 in stellar astrospheres. Derived \dot{M} depends on models . . .

