To: EDGES Group  
From: Alan E.E. Rogers  
Subject: FEKO tests of slot resonances

1] Introduction
The EDGES is extremely sensitive to poor connections on parts of the antenna and ground plane. The study in memo #138 further by looking in more detail at resonant slots. It is well known that RF leakage from enclosures is dominated by leakage at the seams and consequently panels and lids need to be fastened by screws placed a small fraction of a wavelength apart. However, as mentioned in memo #138 the slots in the seams between the screws can resonate at surprisingly low frequencies. For example, a slot 9 inches wide naturally resonant at 980 MHz will resonate at 175 MHz when loaded with 19 pf capacitance across the gap. Resonances can still occur when there is only capacitive contact between the screws and can move down to surprisingly low frequencies.

2] Expected strength of resonances in the spectrum
If the resonant slot is viewed as an antenna the reflected power is given by the radar equation

$$P_r = P_T G_T G_s A_r A_s / (4 \pi r^2)^2$$

$$= P_T A_r^2 A_s^2 / (\lambda^2 r^2)^2$$

Where

$P_r$ = power received  
$P_T$ = power transmitted  
$G_T$ = Gain of transmitter antenna  
$G_s$ = Gain of slot antenna  
$A_r$ = Effective aperture of transmitter antenna  
$A_s$ = effective aperture of slot antenna

$$|S11| = A_r A_s / (\lambda^2 r^2)$$

To estimate the effect on the spectrum consider the reflection of the outgoing wave from the LNA is the antenna which is returned to correlate with the noise waves of the LNA.

In this case

$$P_s = P_{LNA} |1 + S11|$$
Where $\rho$ = correlation coefficient

For example if the outgoing LNA noise is 40K, the correlation coefficient is one and $S_{11}$ is -60 dB the peak to peak “ripple” due to the changing phase of the reflection will be about 80 mK.

Another mechanism is the reflection of the sky noise from the antenna. In this case

$$P_s = P_{sky} \left| 1 + S_{11} \Gamma \right|^2$$

Where $P_{sky}$ is the sky noise and $\Gamma$ is the antenna reflection coefficient. For $P_{sky} = 300 K$, a $-20$ dB reflection coefficient and $S_{11}$ equal to $-60$ dB the peak to peak ripple is about 60 mK.

The effect of the slot resonance should be measurable in the $S_{11}$ for these examples as it is at a level of about 0.05 dB in the difference at resonance for an $S_{11}$ of $-15$ dB.

Figure 1 shows a FEKO simulation for a 6” slot in the middle of the ground plane loaded by 19.2 $\mu F$ in series with 0.1 ohm resistance.

Another effect of a resonance is a change in the antenna beam with frequency around the resonance. In this case the spectrum change will be a function of the local sidereal time.

The resonance of figures 1 and 2 was generated using FEKO and since the slot was located in the center of the ground plane it produced a change in $S_{11}$ of 0.05 and produced an estimated effect on the spectrum due to reflection of the LNA noise of about 10K peak to peak whereas the effect on the spectrum due to frequency dependence of the beam was about 40 K peak to peak. As the resonant slot is moved away the effects on the spectrum due to a change in $S_{11}$ are expected to decline with distance squared while the effects on the beam scale with distance at least for a point source which dominates the sky noise. There are many other factors which will reduce the effects. These include orientation and resistive loss in the slot.

A resonance shown in Figure 3 has been observed in the EDGES high band data started around 2 May 2015. It has a complex spectrum centered at about 175 MHz. It is relatively weak with a maximum of about 100 mK peak to peak. It varies with Galactic Hour Angle (GHA). The complex spectrum might be the result of the two or more cavity slots resulting from poor contact between the antenna baseplate and the rest of the ground plane. The resonance is not evident in the $S_{11}$. 
Figure 1. The amplitude (thinnest line), phase (thicker line) and spectrum example (thickest line)
Figure 2. Effect of the resonance on the spectrum from its effect on the beam.
Figure 3. Resonance at 175 MHz shows signature change with GHA.