VLBI Basics

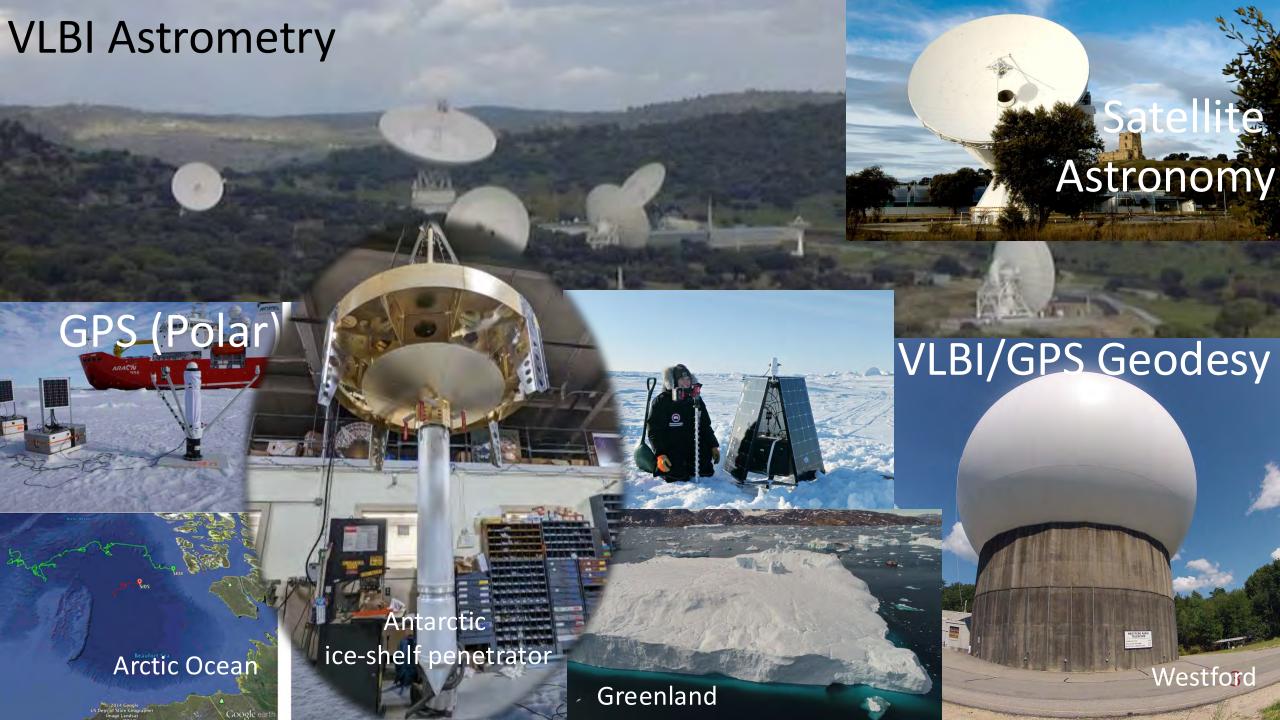
Pedro Elosegui, MIT Haystack Observatory

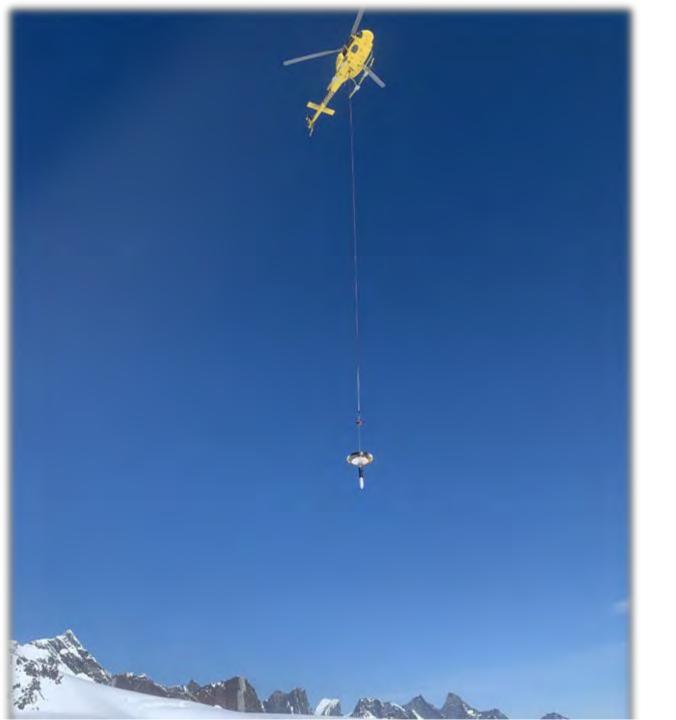
With thanks to many of you (here and "out there")



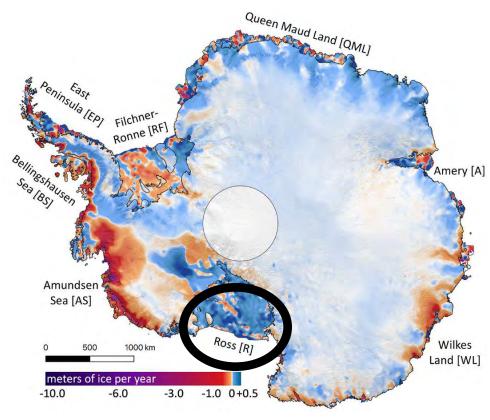








Antarctic ice penetrator: Ross Ice Shelf

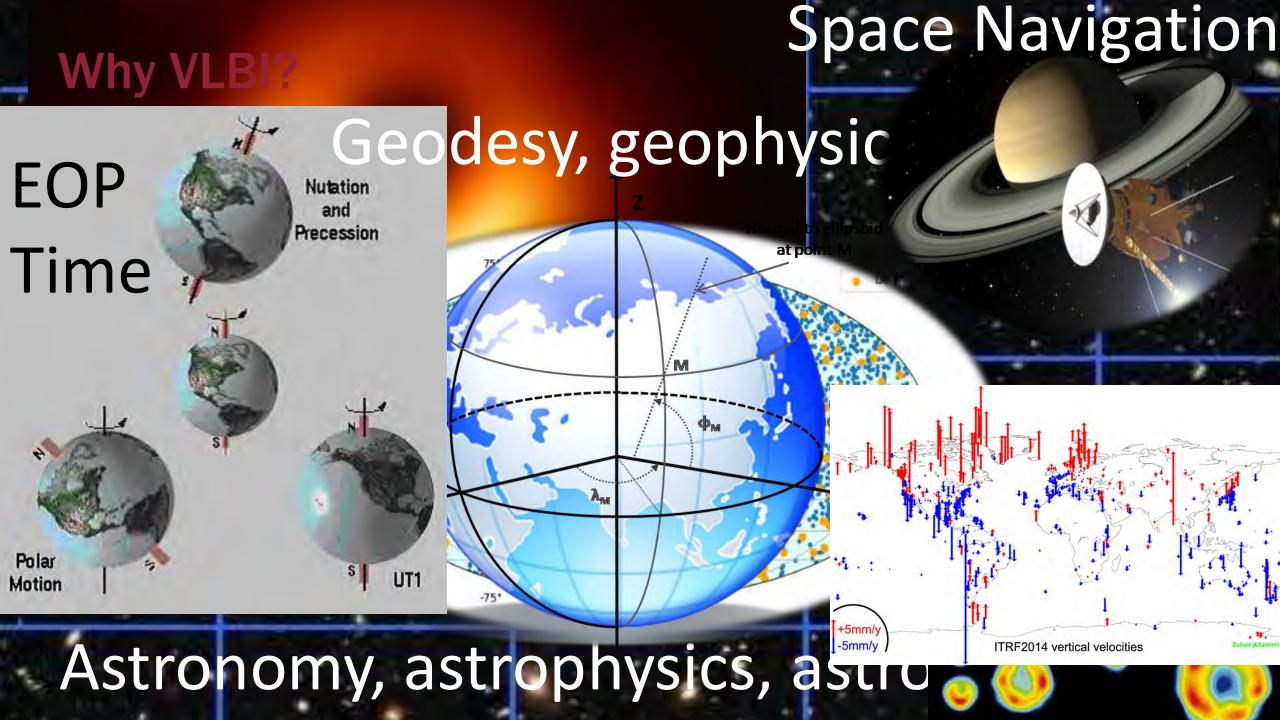




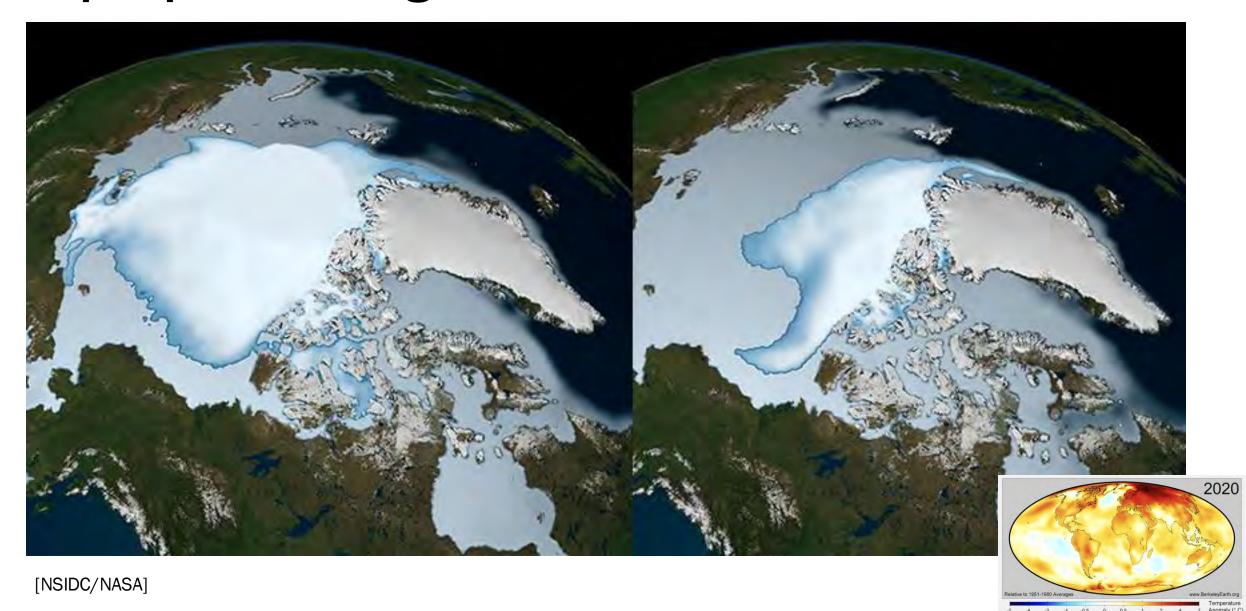
Outline for today

Motivation: WHY do we do VLBI?

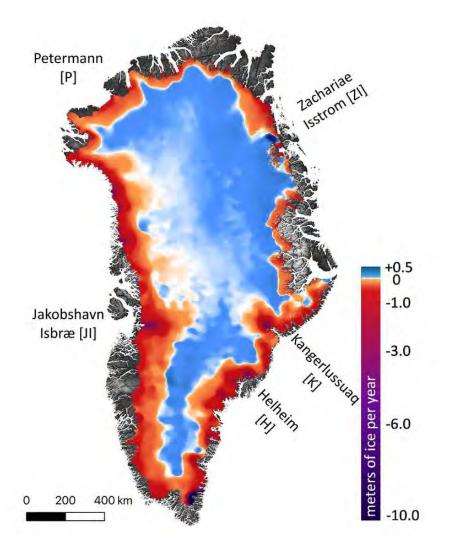
- Hands-on: HOW do we do VLBI?
 - Geodetic radio telescopes
 - VLBI vs. GPS concept
 - Station requirements
 - VLBI digitization
 - VLBI correlation
 - Geodetic post-processing and VGOS precision

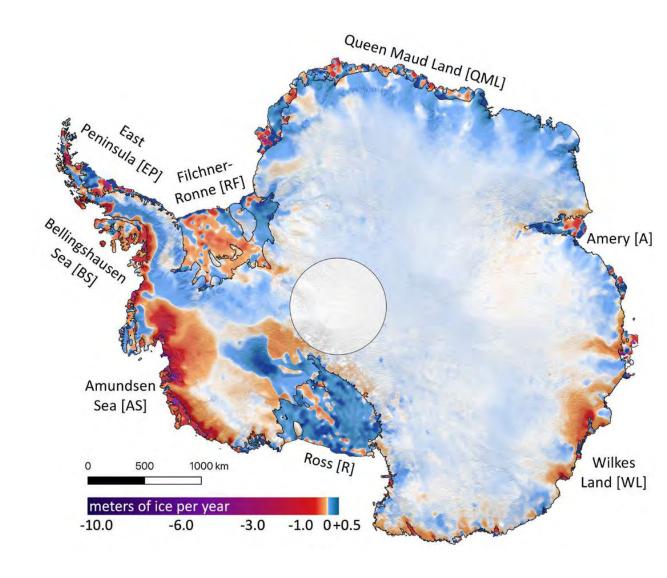


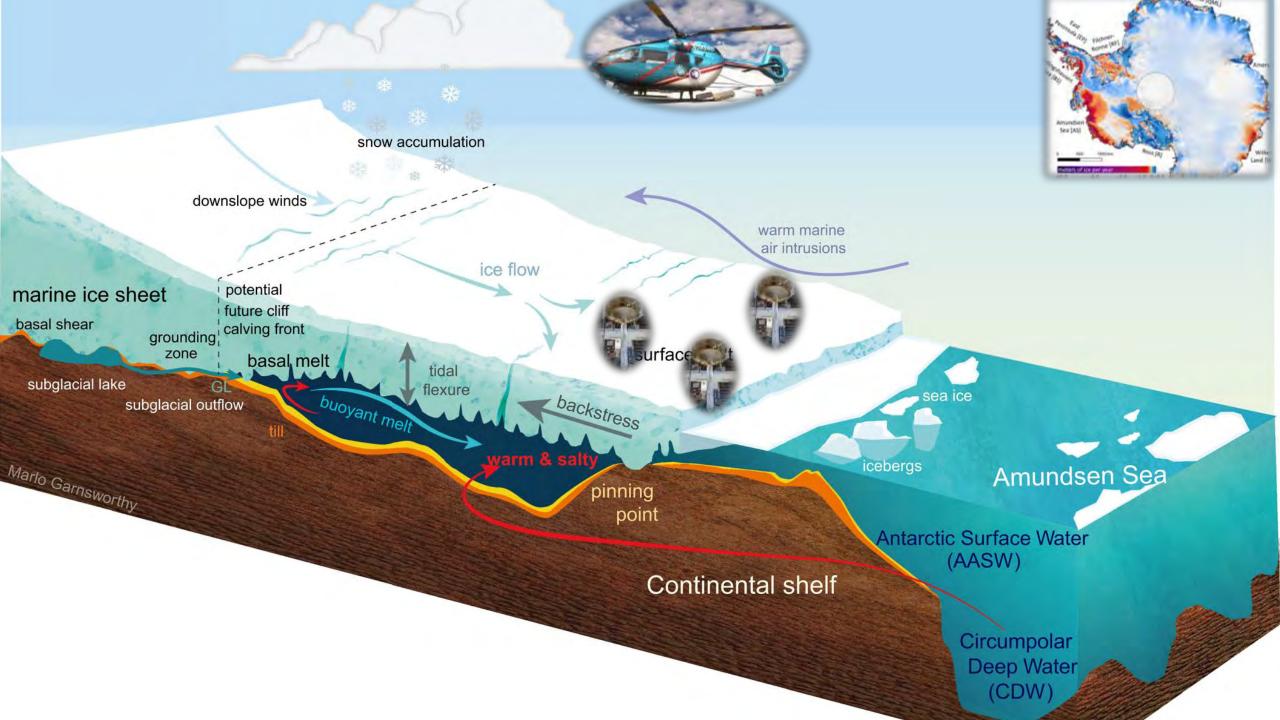
Rapid polar changes: Arctic sea ice loss

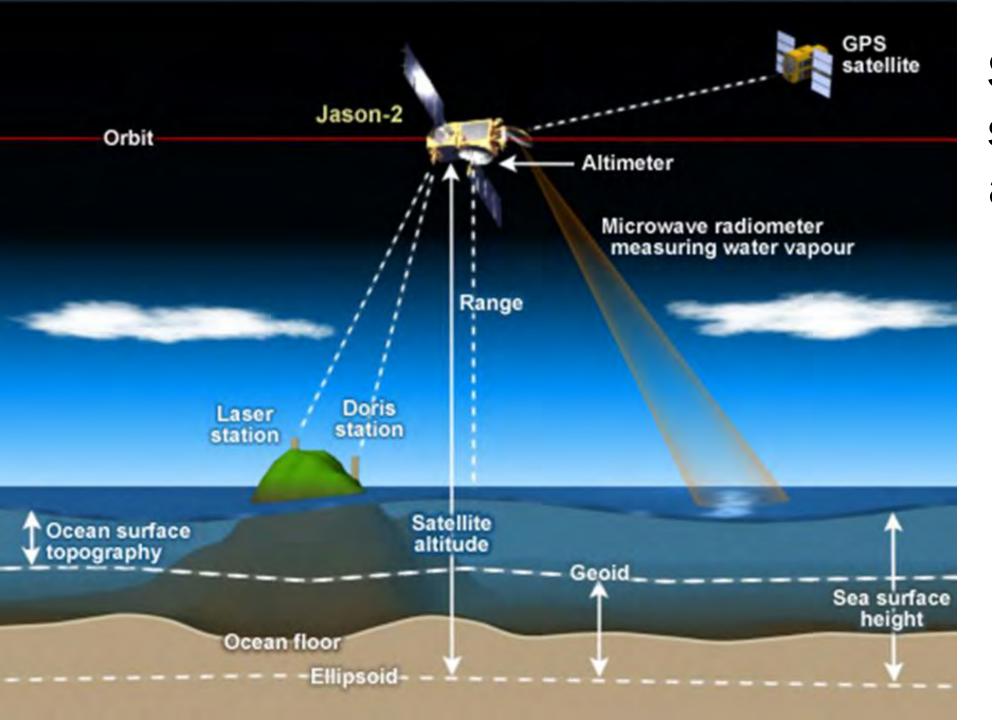


Rapid polar changes: Ice sheet mass loss



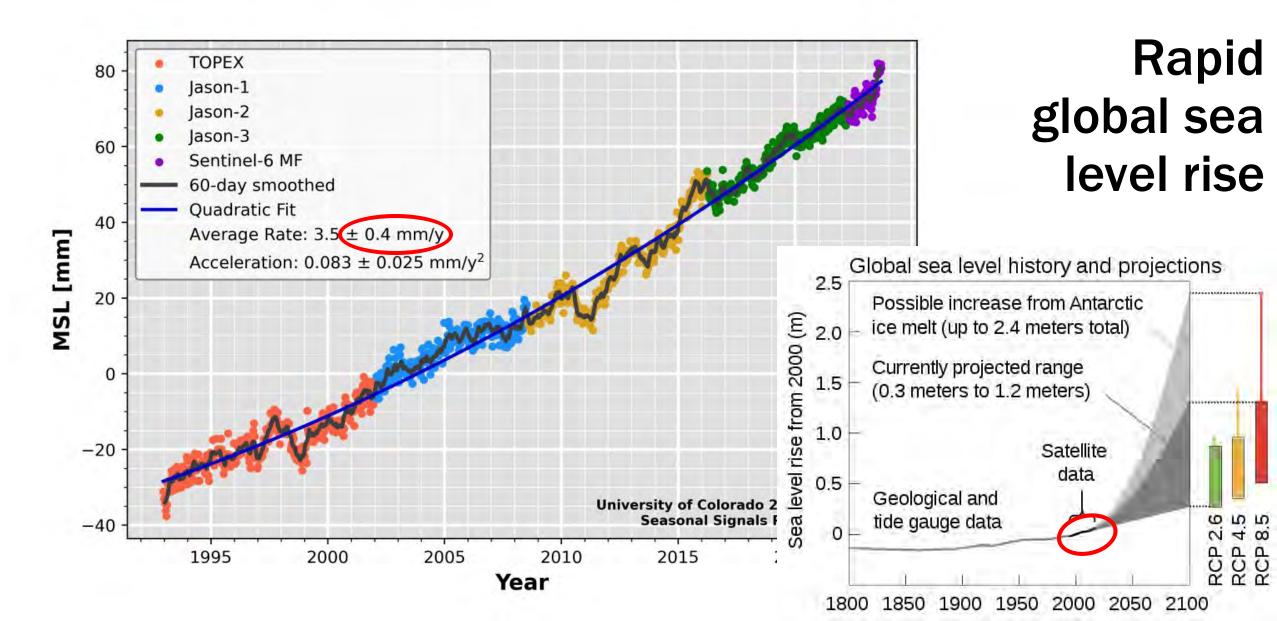


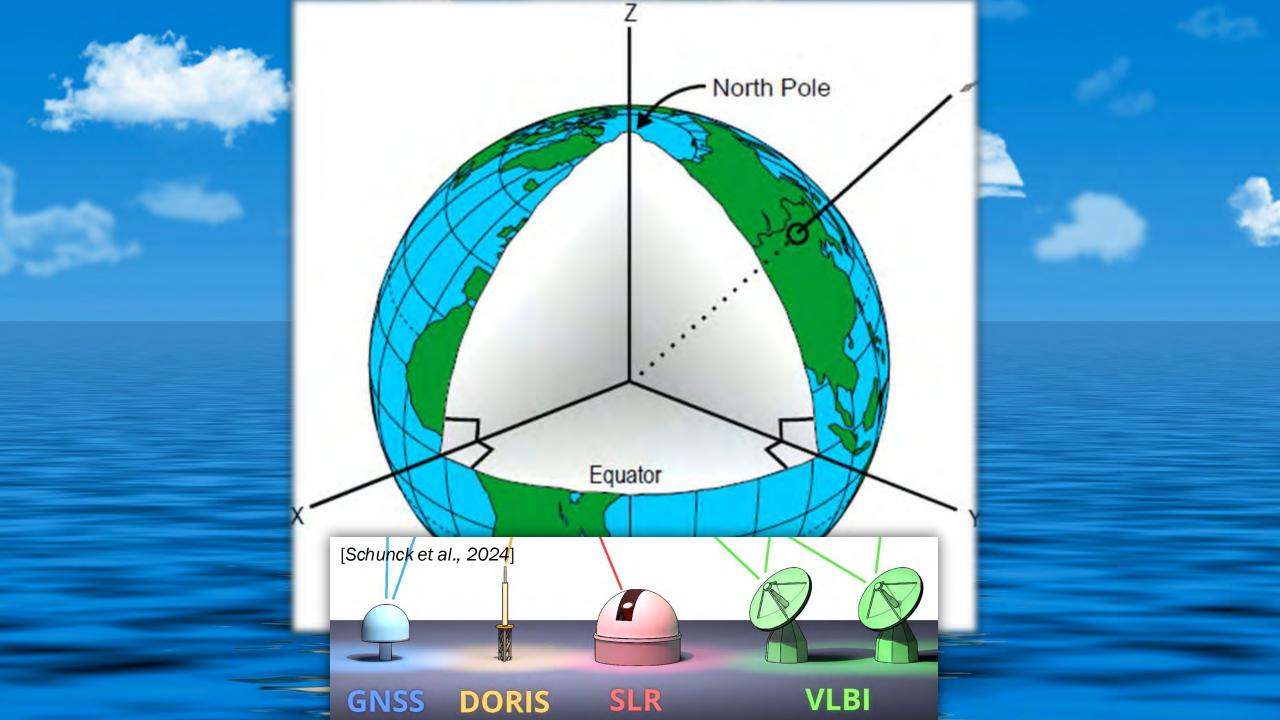




Sea level, satellite altimetry

Global mean sea level (MSL) from satellite altimetry





Why VLBI?

CLIMATE CHANGE IS THE DEFINING CHALLENGE OF OUR TIME

- Climate needs geodesy, geodesy needs VLBI/VGOS, VGOS needs you collecting the very best quality data you can.
- While staying humble, the contribution of each one of you (of us all, really) is terribly important.
- But please do not panic if you miss one scan, one session, something bigger; reflect, learn, connect, come back stronger.





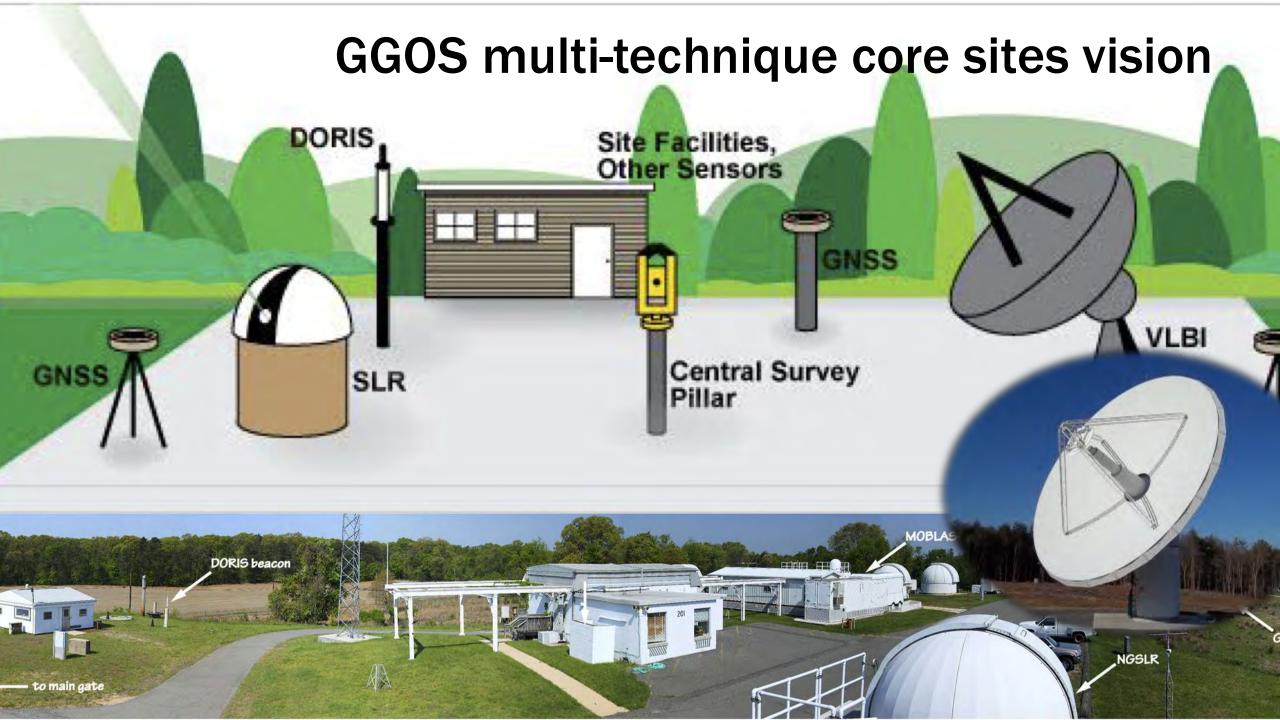
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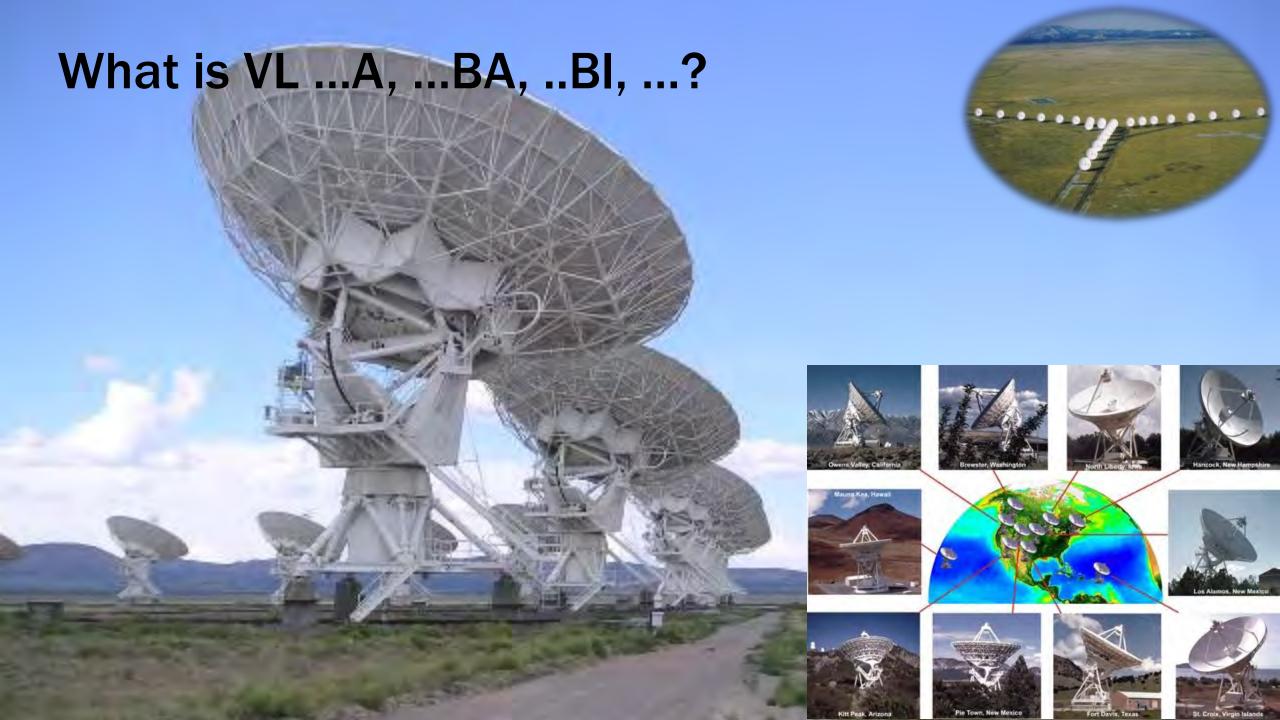
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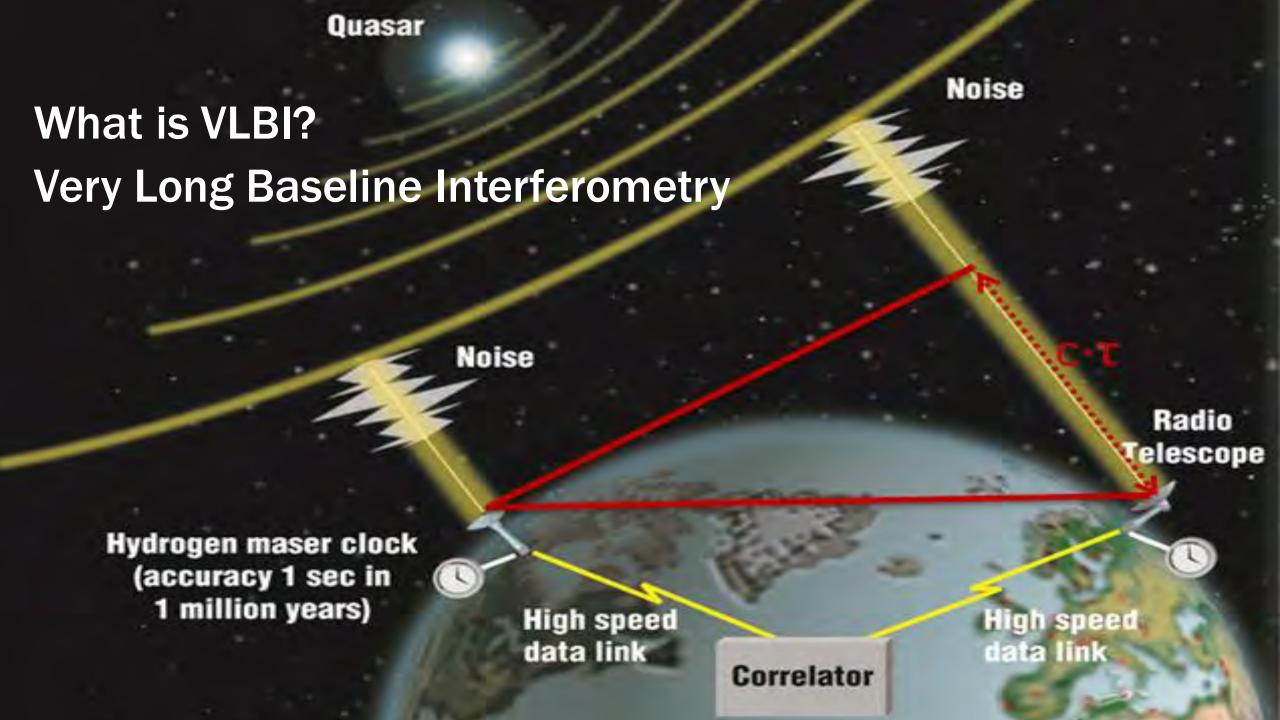






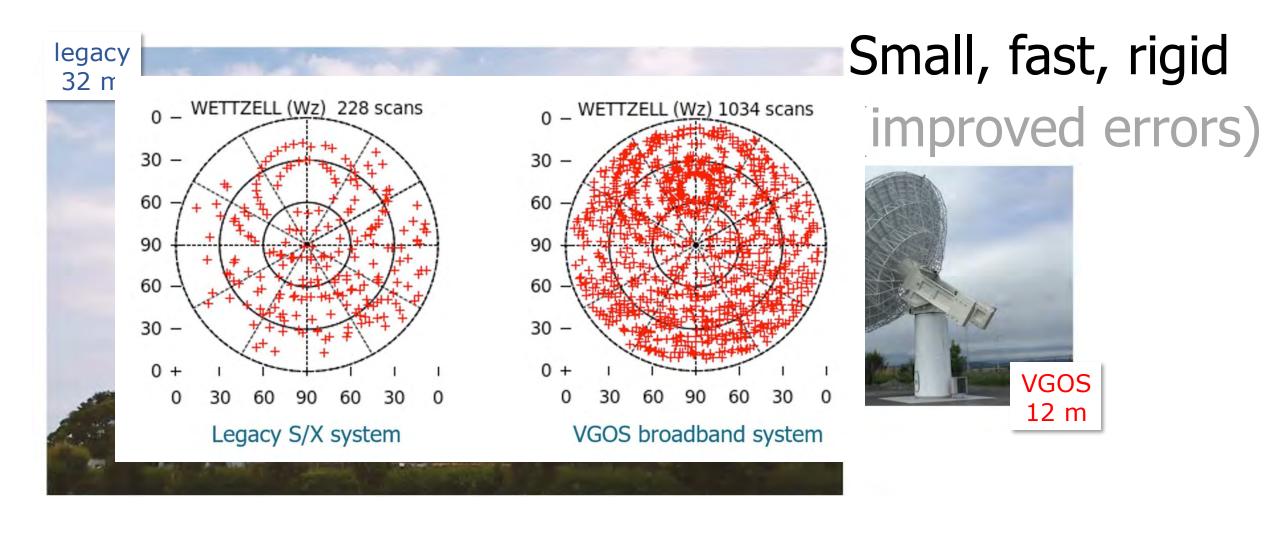




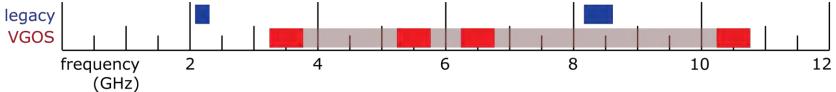


-180° NORTHERN **HEMISPHERE** 1500 SOUTHERN VLBI Global **HEMISPHERE HOBART KPGO** Observing ISHIOKA **System** (VGOS) "today" MGO GGAO NY-ÅLESUND WESTFORD ONSALA WETTZELL **FORTALEZA** YEBES 30° 300 **HRAO**

VGOS virtues (vs. "legacy S/X") in a nutshell



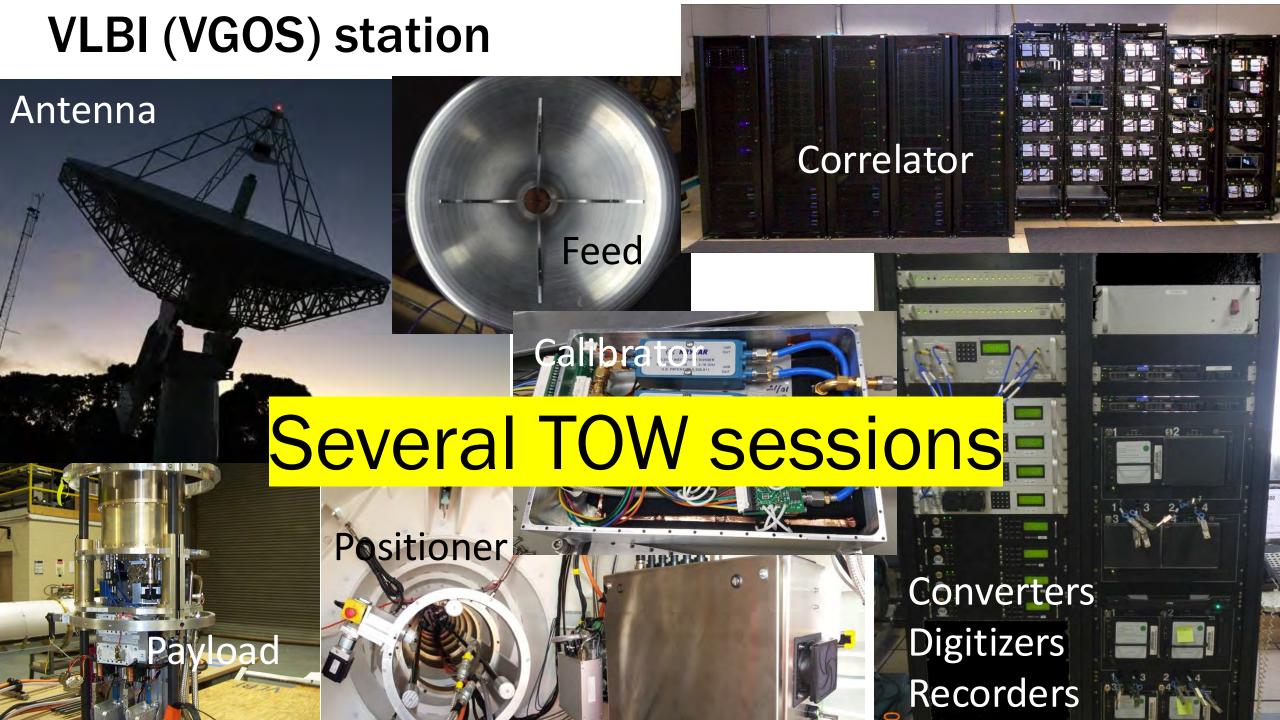
Broad bandwidth (better sensitivity)



Basic elements of VLBI (geodesy)

- Antennas
- Receivers
- Analog and digital stages
- Recorders and data transport
- Correlation, post-processing
- Imaging, positioning, orientation





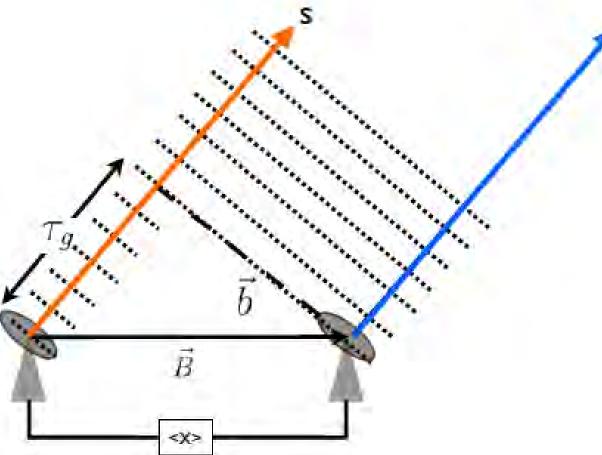


System

Relative phase $\phi_g = 2\pi\nu\tau_q$ shift

Geometric delay

$$au_g = \vec{B}.\hat{s}/c$$





High-precision geodetic science

Observation = Model + Error

$$\tau = \tau_g + \tau_{clk} + \tau_{ion} + \tau_{trop} + \tau_{inst} + \tau_{rel} + \tau_{other} + \epsilon$$

Signal (geometry => position, orientation) rest is all "noise"









GNSS



Practical VLBI observational goals

High-precision geodesy means observable with small error

$$\sigma_{\tau} = \frac{1}{2\pi} \cdot \frac{1}{SNR \Delta \nu}$$

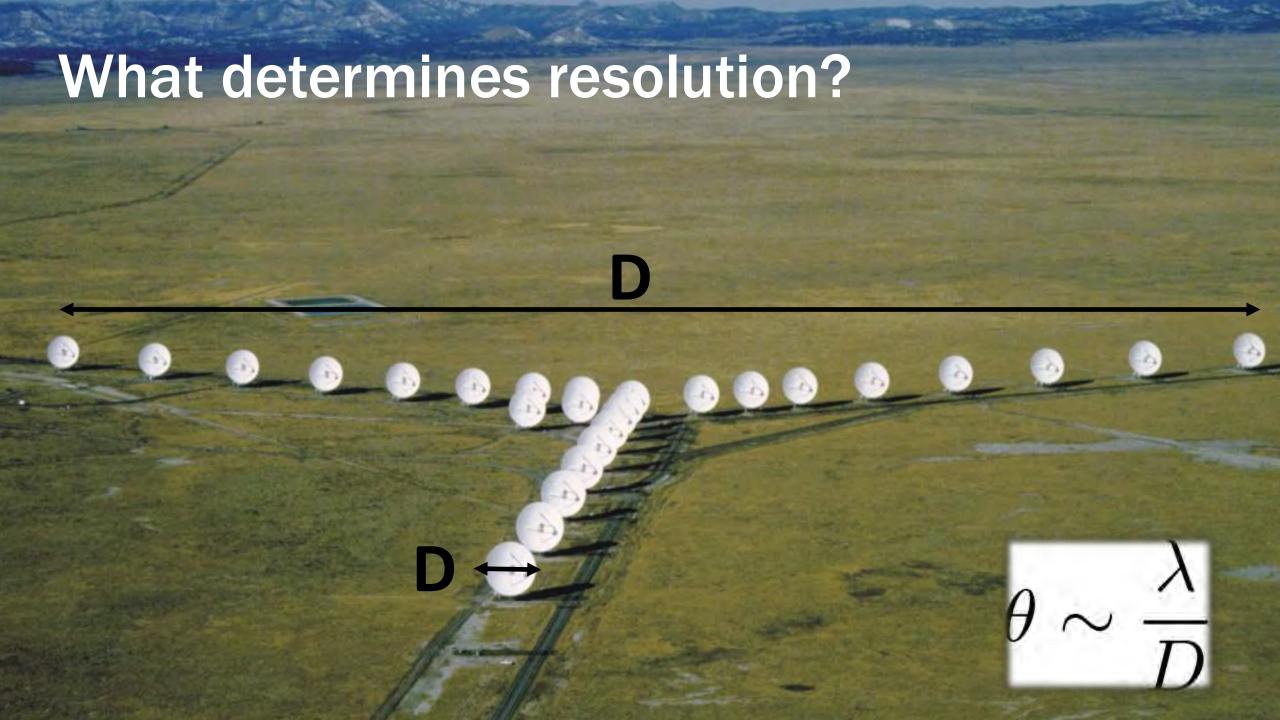
Sensitivity = ability to "see" faint objects (interferometer, Jy)

$$\Delta S = \frac{1}{\eta_s} \cdot \sqrt{\frac{SEFD_i \cdot SEFD_j}{2\Delta\nu \, \tau_{acc}}}$$

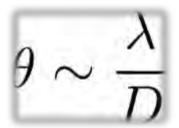
Resolution = ability to "see" details in distant objects

What determines sensitivity?

- Amount of energy collected (Ta, gain, efficiency)
 - Size and quality of the collecting area
 - but cost of bigger antennas tends to increase as D^2.7 (i.e., doubling antenna diameter raises price by ~6!)
 - Bandwidth of the energy spectrum
 - sensitivity improves as square root of observed bandwidth, cost effective
- Quietness of the receiving detectors (Tsys)
 - many receivers are already approaching quantum noise limits, or are dominated by atmospheric noise

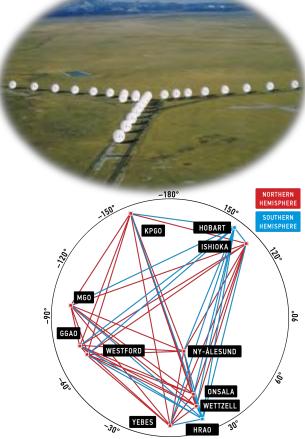


A few resolution examples



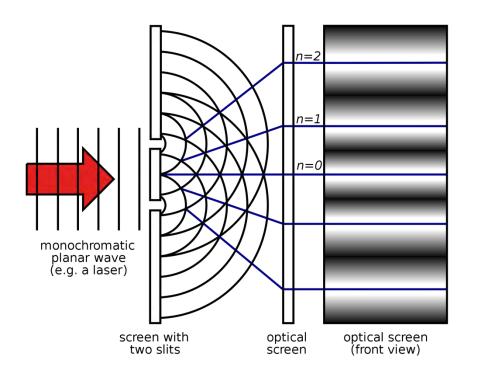
	D	λ	θ	Moon surface
VGOS antenna	12 m	3 cm (10 GHz)	10 arcmin	1000 km
Effelsberg	100 m	1 cm (30 GHz)	20 arcsec	
VLA	35 km	1 cm	0.1 arcsec	
VGOS	10,000 km	3 cm	0.6 mas	1 m

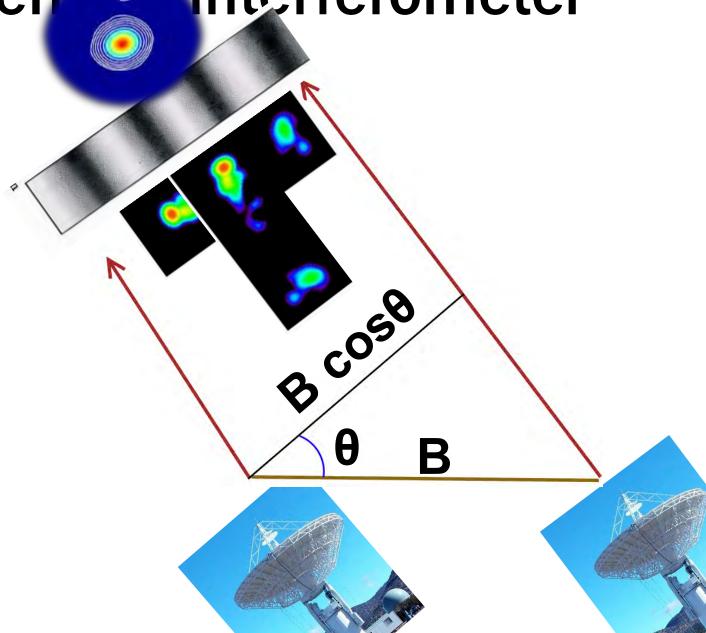




Principle of two-element interferometer

Young double-slit experiment



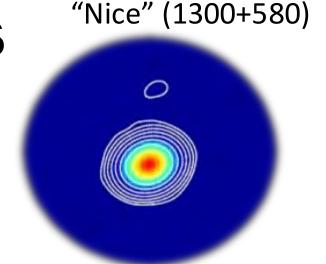


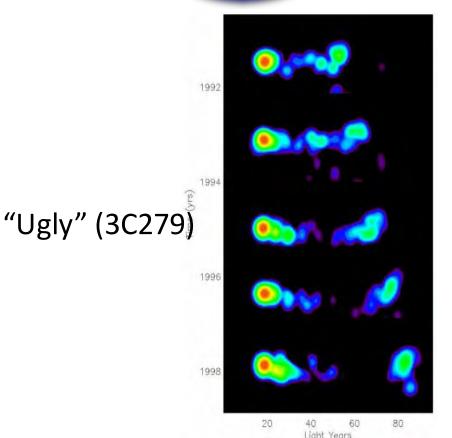
Geodetic VLBI radio sources

 VLBI geodesy requires sources that are bright, compact, and "stable" both in time and frequency; a challenge

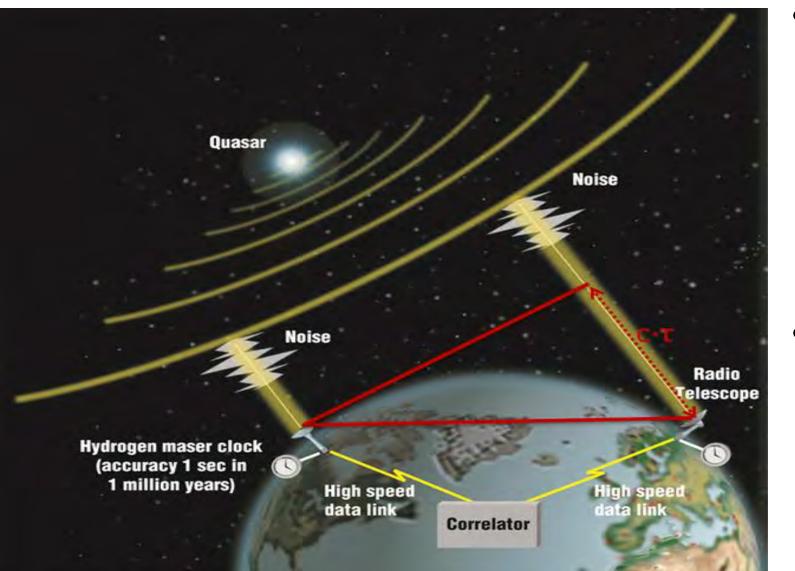
 The total number of available useful sources for current geodetic-VLBI capabilities is small (<~1000)

 VGOS, with its improved sensitivity, should significantly improve the number of available sources





Principle of (geodetic) VLBI/VGOS



 Measure time-of-arrival difference (delay) accurately

$$\sigma_{\tau} = \frac{1}{2\pi} \cdot \frac{1}{SNR \, \Delta\nu}$$

 mm-level positioning requires delay precision of a few picoseconds (3 ps = 1 mm)

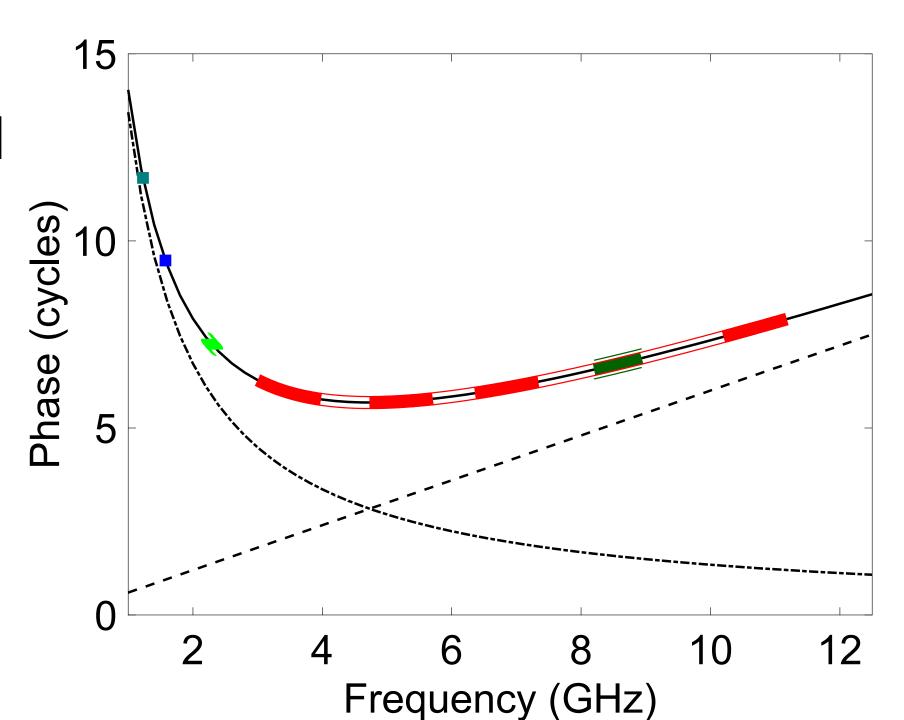
VGOS station requirements

- Observing "noise" from quasars (contaminated by various noise sources)
- Measuring a (group) delay (a time measurement) whose precision is inverse of spanned bandwidth
 - Requires wideband feeds and receivers (VGOS 2-14 GHz)
 - Multi-band systems to correct for ionosphere delays



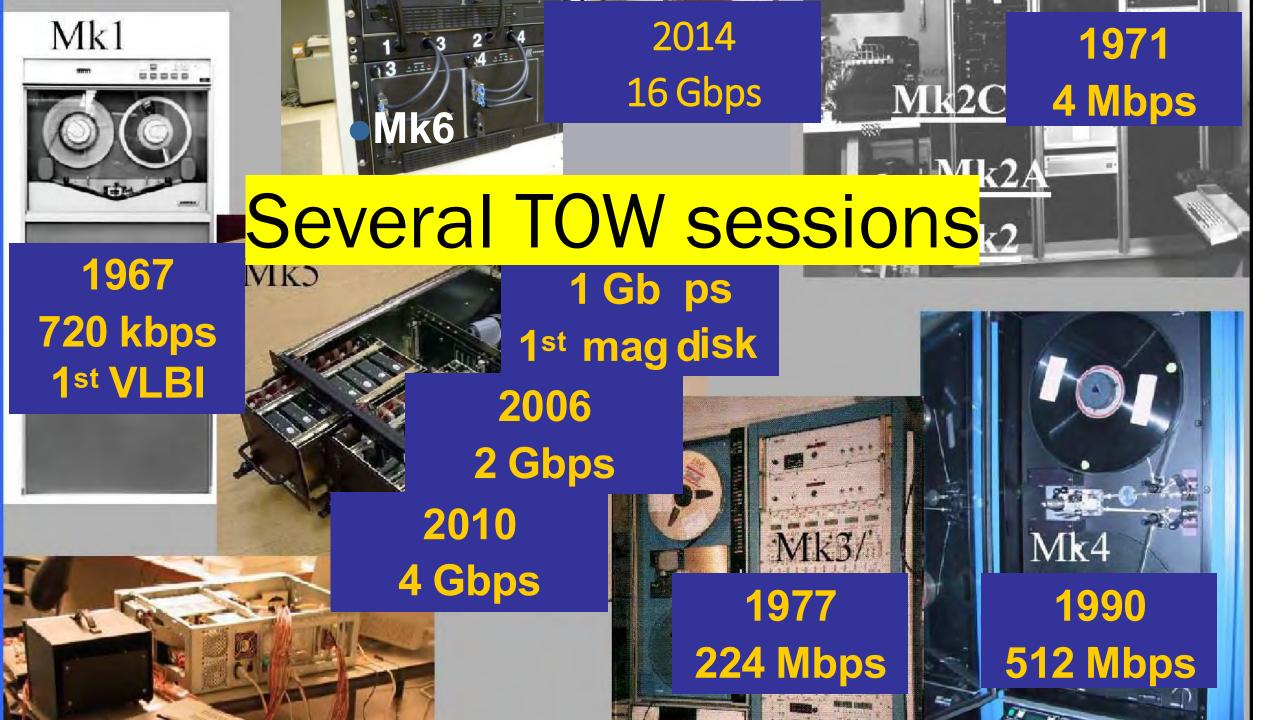


VGOS broadband delay



VGOS station requirements

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- Measuring a (group) delay (a time measurement), whose precision is inversely of spanned bandwidth
 - Requires wideband feeds and receivers (VGOS 2-14 GHz)
 - Multi-band systems to correct for ionosphere delays
 - Low-noise receivers (low SEFD, antenna efficiency, cryogenics)
 - Antennas that are small, efficient, and fast (atmosphere)
 - High-speed recording for high SNR via large bandwidth (Nyquist)



VGOS station requirements

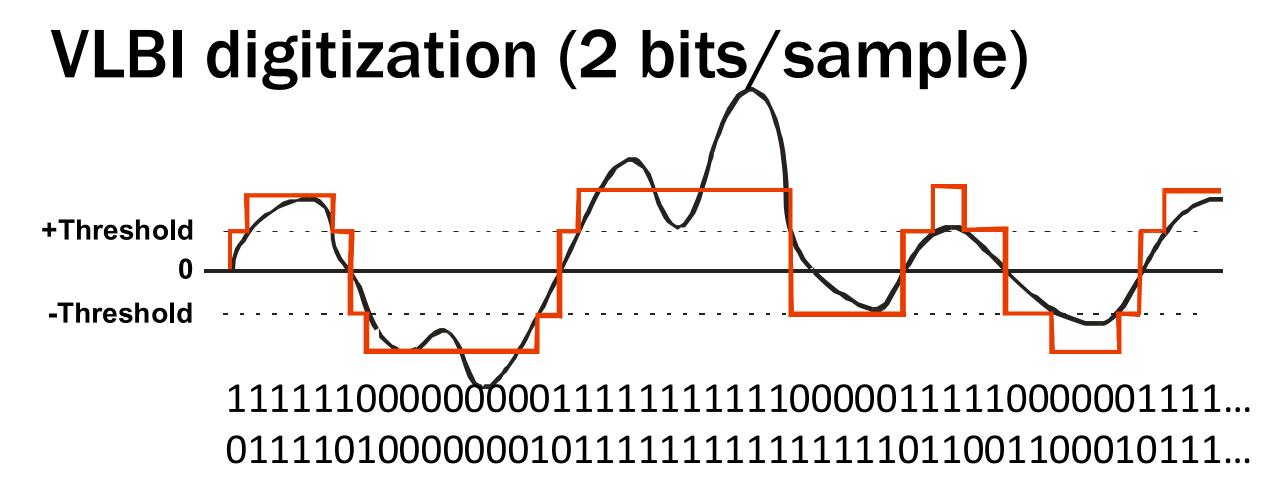
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 - High-speed recording for high SNR via large bandwidth (Nyquist)
 - Hydrogen maser frequency standards
 - Accurate time synchronization (to ~300 nsec with GPS time)
 - Instrumental calibrations (cable delays and phase calibration)

What is the recorded VLBI data?

Answer: precisely timed samples of noise, usually nearly pure white, Gaussian noise!



- Interesting fact: normally, the voltage signal is sampled with only 1 or 2 bits/sample
- Big consequence, it is near incompressible
- But another important consequence, it is not a big deal to lose a small amount of data



- The spectrum of a Gaussian-statistics bandwidth limited signal may be completely reconstructed by measuring only the sign of the voltage at each Nyquist sampling point (Van Vleck, 1960) [For 32-MHz VGOS channels, that is 64 Msps = 20 ns]
- Relative to infinite bit sampling, VLBI SNR at 1 and 2 bits/sample is only 63% and 87%, respectively, better compensated by increasing recording bandwidth

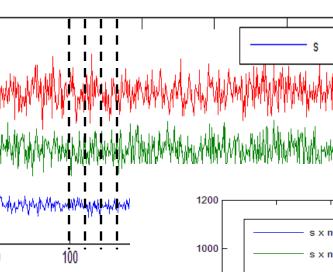
VLBI correlation (of weak signals)

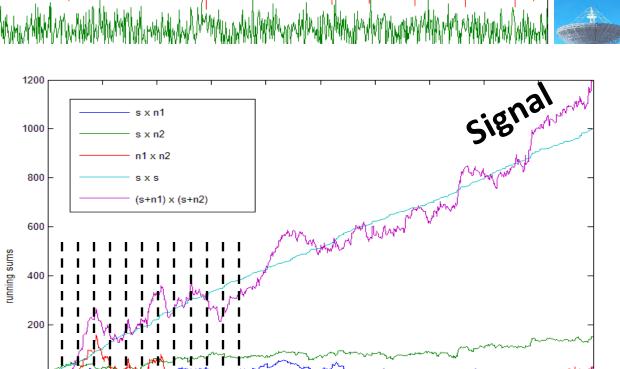
Receiver 1 noise $n_1(t)$

Receiver 2 noise $n_2(t)$



Signal s(t)





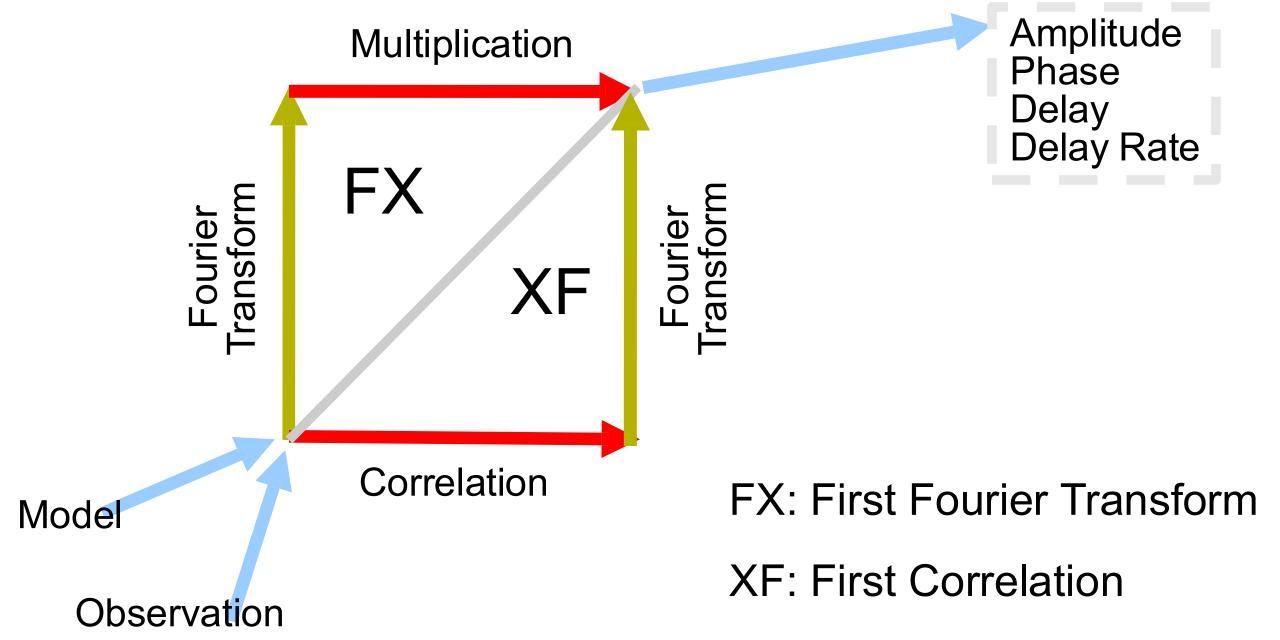
700

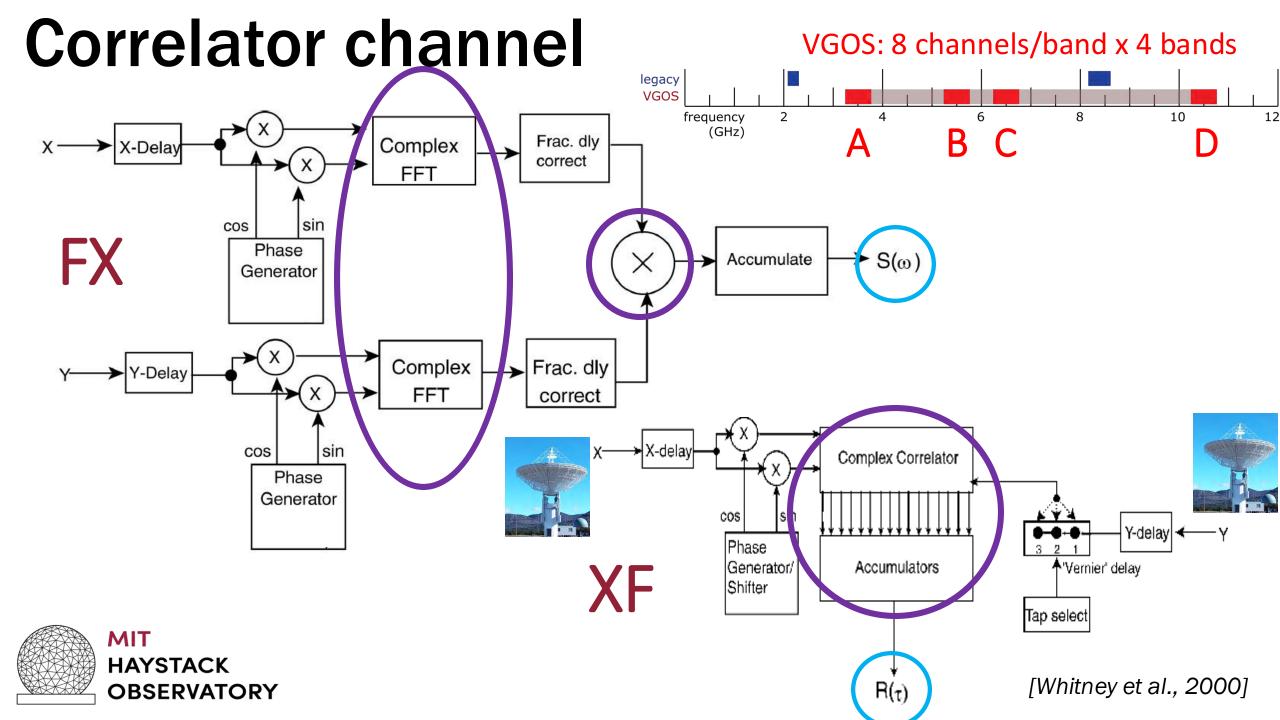
Time-lag correlation = product and addition (pulling signal from the noise):

$$(s + n_1) (s + n_2) = s^2 + n_1 s + n_2 s + n_1 n_2$$

(Earth rotation adds complexity because causes time-ofarrival difference and Doppler shift to continually change)

Correlators: two flavors of processors





Combine channels via "bandwidth synthesis"

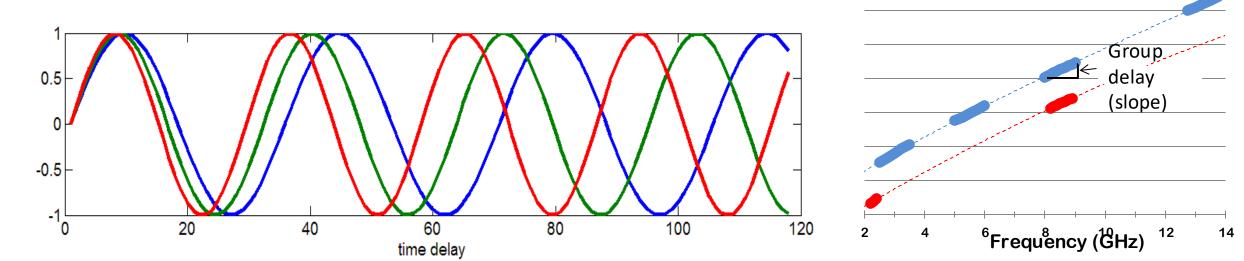
The goal is to measure the group delay, defined as $d\theta/d\omega$

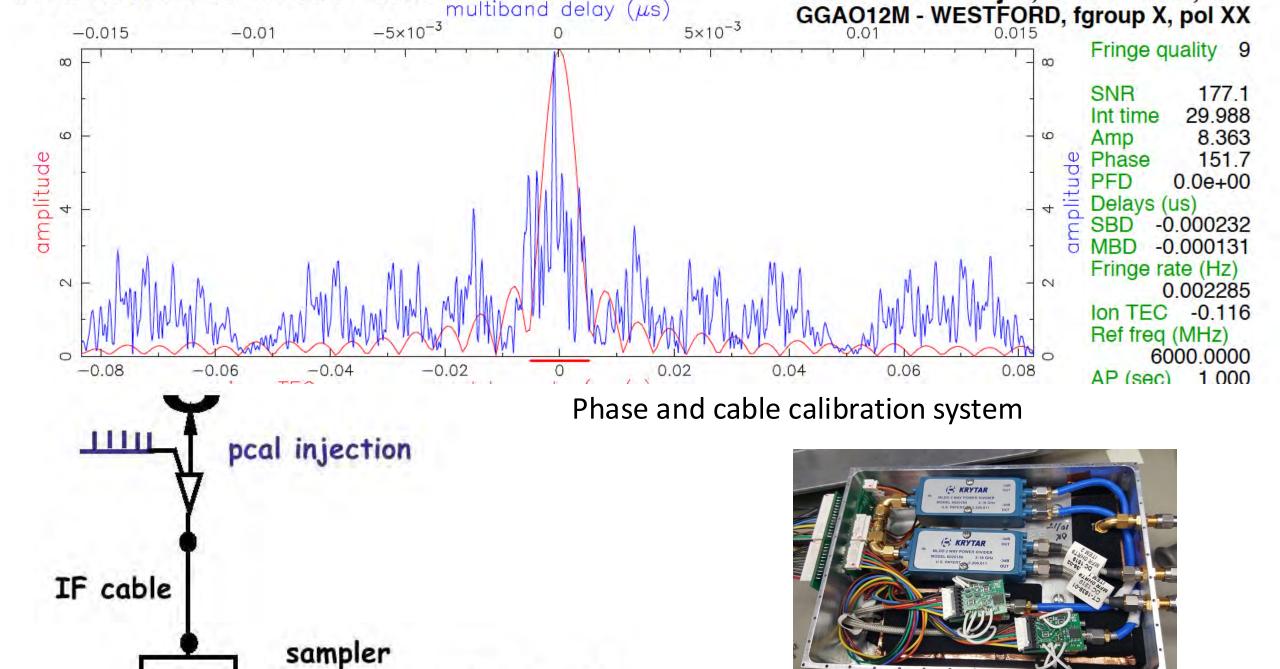
$$\phi_g = 2\pi\nu\tau_g$$

First, we must measure the observed fringe-phase difference for each of the observed frequency channels:

For a given delay, the higher the fringe frequency, the

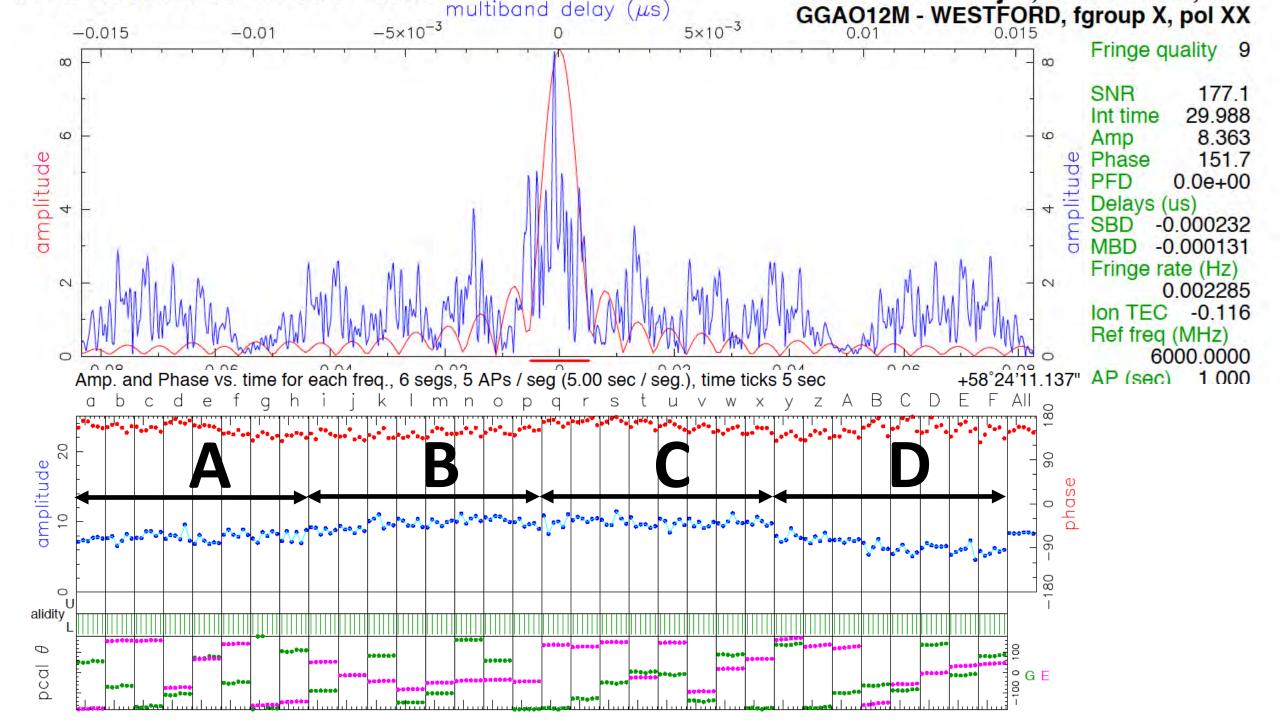
greater time-rate change in phase:

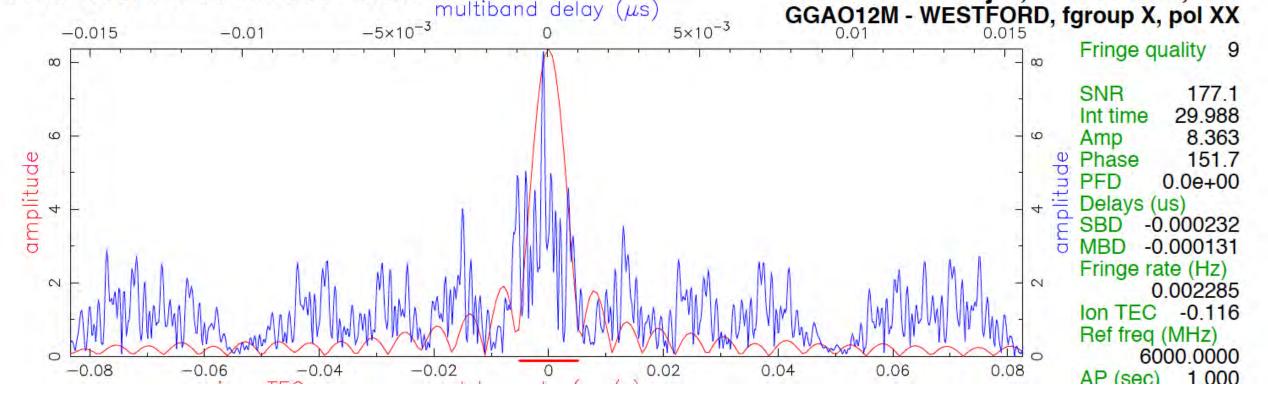




pcal extraction

DAR





Observables for each baseline-scan:

- Correlation Amplitude
- Correlation Phase (generally 2π ambiguous)
- Total Group Delay
- Total Delay Rate



All tied to a precise UT epoch



High-precision geodetic science

Observation = Model + Error

$$\tau = \tau_g + \tau_{clk} + \tau_{ion} + \tau_{trop} + \tau_{inst} + \tau_{rel} + \tau_{other} + \epsilon$$

Signal (geometry => position, orientation) rest is all "noise"



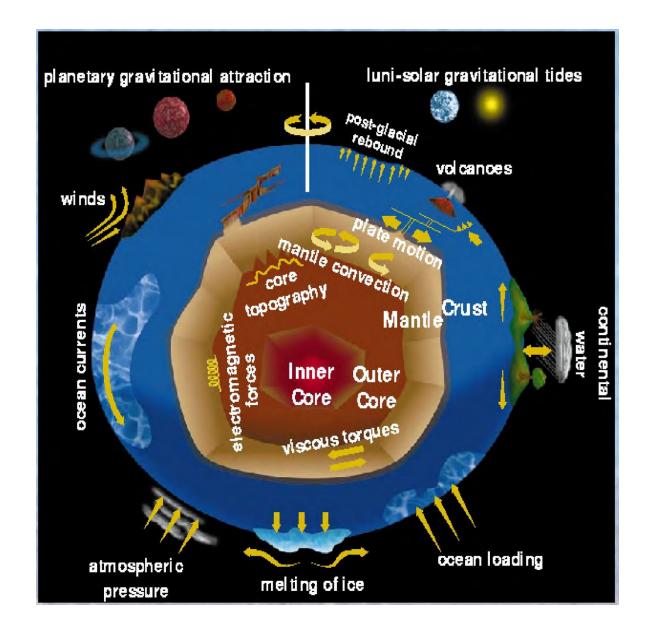






GNSS

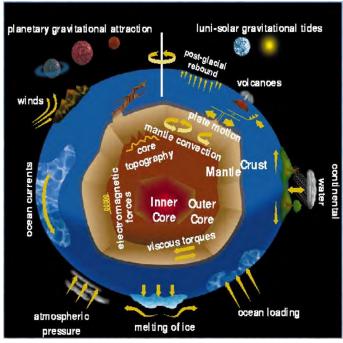




Living on a dynamic Earth

The ensemble of observables from a session are only useful if a detailed and highly sophisticated model of the Earth and its messy motions exists

Modeling the dynamic Earth

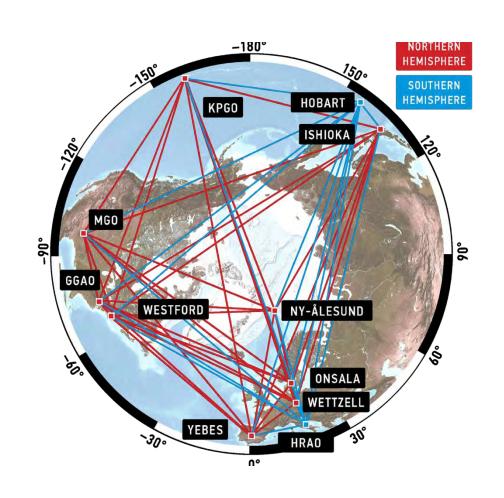


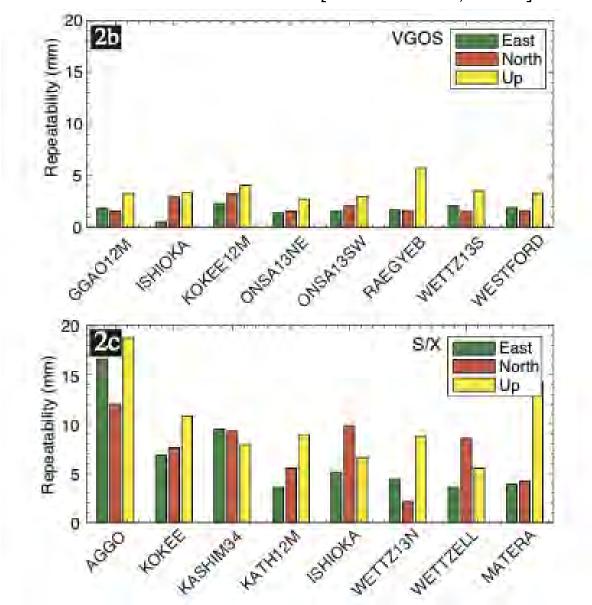
Adapted from Sover et al., (1998)

Item	Approx Max.	Time scale
Zero order geometry.	6000 km	1 day
Nutation	~ 20"	< 18.6 yr
Precession	$\sim 0.5 \text{ arcmin/yr}$	years
Annual aberration.	20"	1 year
Retarded baseline.	20 m	1 day
Gravitational delay.	4 mas @ 90° from sun	1 year
Tectonic motion.	10 cm/yr	years
Solid Earth Tide	50 cm	12 hr
Pole Tide	2 cm	~1 yr
Ocean Loading	2 cm	12 hr
Atmospheric Loading	2 cm	weeks
Post-glacial Rebound	several mm/yr	years
Polar motion	0.5 arcsec	$\sim 1.2 \text{ years}$
UT1 (Earth rotation)	Several mas	Various
Ionosphere	~ 2 m at 2 GHz	All
Dry Troposphere	2.3 m at zenith	hours to days
Wet Troposphere	0-30 cm at zenith	All
Antenna structure	<10 m. 1cm thermal	
Parallactic angle	0.5 turn	hours
Station clocks	few microsec	hours
Source structure	5 cm	years

VGOS positioning accuracy

[Mondal et al., 2021]

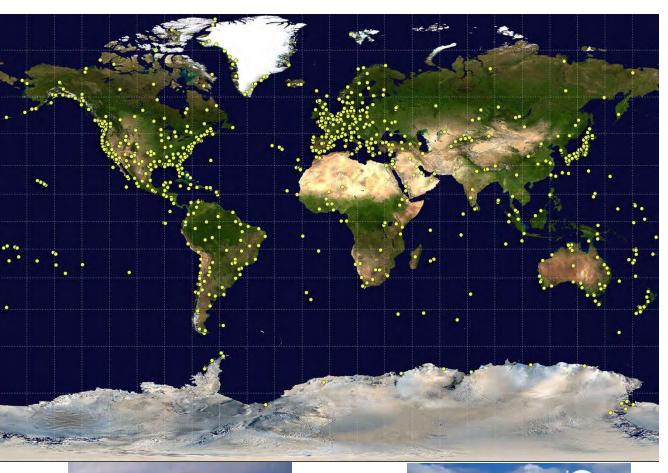


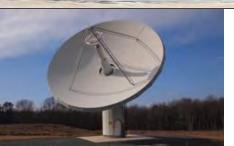




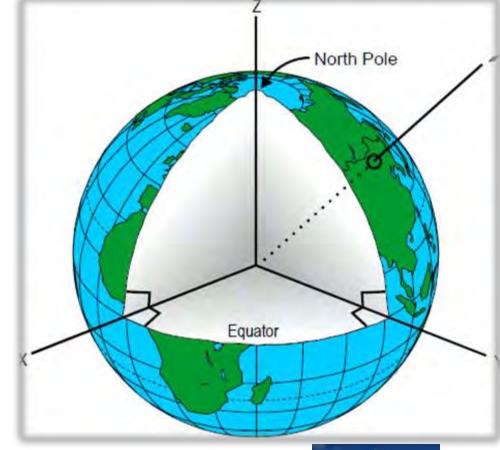
VGOS network rollout Ny-Alesund Onsala Svetloe Metsahovi Badary Wettzell Urumqi Westford Flores Zelenchukskaya Ishioka Yebes Matera **GGAO** Santa Maria McDonald Sheshan Kokee Gran Canaria Kanpur Chiang Mai Songkhla Fortaleza Katherine Tahiti Yarragadee Hartebeesthoek **AGGO** Hobart operational antenna built, signal chain work in planning stage

Improved Terrestrial Reference Frame and EOP















DORIS

In summary

- WHY we do VLBI/VGOS
 - Climate change is the defining challenge of our time
- HOW we do it
 - Geodetic radio telescopes
 - VLBI vs. GPS concept
 - Station requirements
 - VLBI digitization
 - Correlation
 - Geodetic post-processing and VGOS precision





And that's pretty much it for today

IVS Technical Operations Workshop



Have a wonderful TOW week!

