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To: EDGES Group

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Subject: Additive and multiplicative terms in foreground, ionosphere and antenna loss.

Multiplicative terms are the scale spectral index and “gamma” of the foreground from

$$T_{sky} = af^{s+\gamma \log f}$$

$$\text{So that } \log(T_{sky}) = a + s \log f + \gamma (\log f)^2$$

Where  $T_{sky}$  = sky temperature

s = spectral index

$\gamma$  = “gamma”

$f$  = normalized frequency

$a$  = sky temperature for  $f = 1$

Other multiplicative terms are the ionospheric absorption and antenna beam correction factor since these terms act on the foreground sky temperature. Additive terms are the resistive loss, antenna ground loss and ionospheric emission since those depends on the ambient and electron temperature. In the case of the emission from the ionosphere the antenna temperature,  $T_A$  is

$$T_A = T_{sky} + \tau_0 T_e f^{-2.0}$$

where  $\tau_0$  is the ionosphere opacity and  $T_e$  is the electron temperature.

Since the effects of both the multiplicative and additive are small there is little difference in fitting the antenna temperature directly or fitting the log of the antenna temperature. It is point out however that the basis function number 4 is memo 118 is for the departure of the spectral index from -2.5 and another basis function

$$(\log f)^2 f^{-2.5}$$

Is needed for “gamma”. Early tests with the calibrated data from EDGES-2 indicate that the separate basis functions for point sources and free-free emission may not be needed when the “gamma” term is included. For example, a fit using only 3 basis functions shown in Fig. 1. has rms residual of 310 mK in recent data from EDGES-2 when the Galaxy is mostly below the horizon.

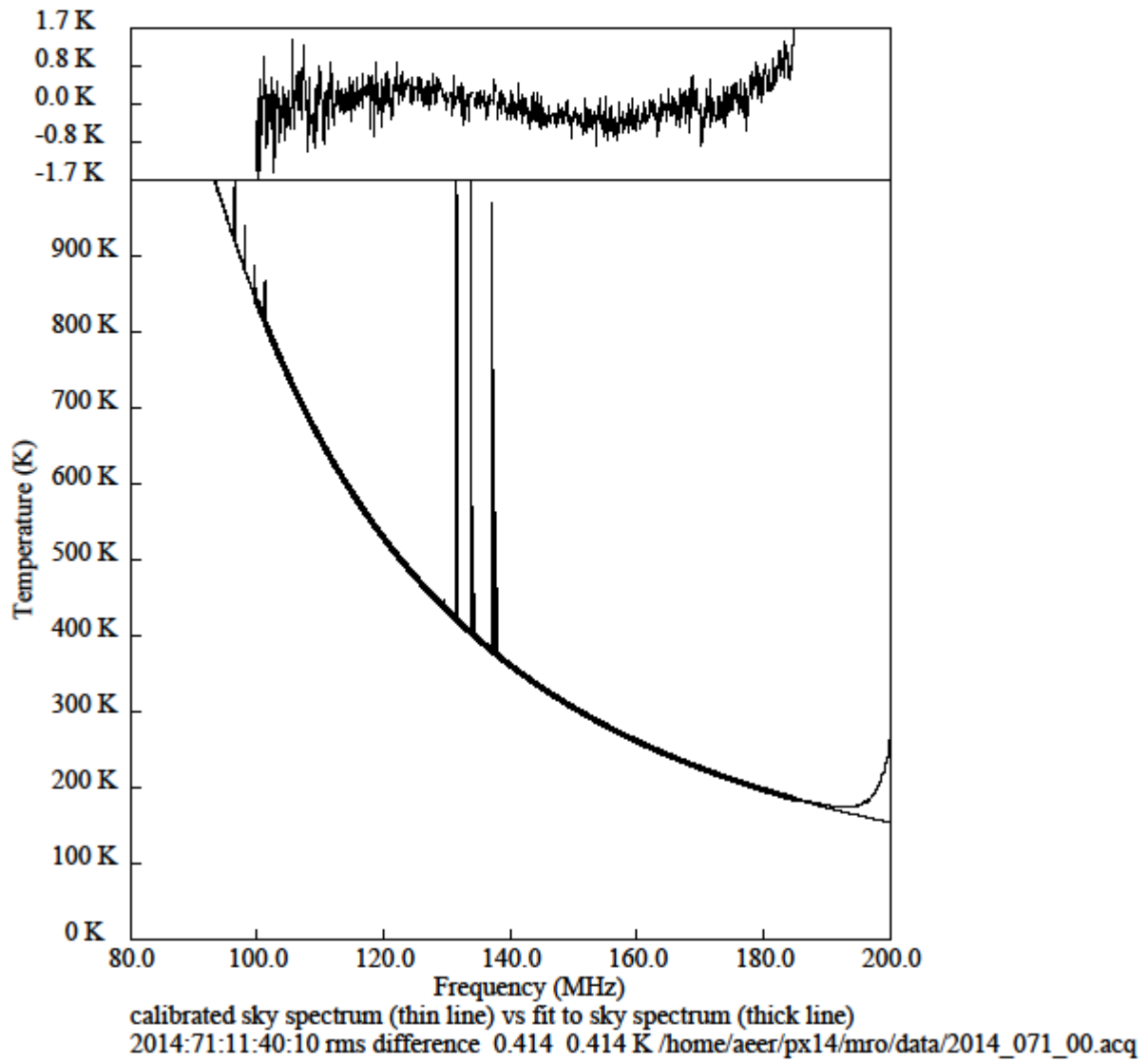


Figure 1. 3 term fit to data for 11 hours before transit of Galactic center.