To: RFI Group  
From: Alan E.E. Rogers  
Subject: Estimate of systematic errors in search for EOR global step

In memos 15 and 16 I described how a small antenna structure might respond gradually with frequency so that the global step could be detected in the residuals to a polynomial fit to the total power data. Figure 1 is a diagram which shows the concept of the system. Figure 2 shows the residuals to a polynomial fit to the receiver output which includes an EZNEC modeling of the “fat” dipole. In order to maintain sufficient numerical accuracy in the polynomial the fitting function used was

\[
z(f) = \left( s(f) - \sum_{k=0}^{N-1} a_k b^k \right)
\]

where \( b = 1024(f - f_{\text{start}})/(f_{\text{stop}} - f_{\text{start}}) \) in place of expression in memo 16. In addition the actual polynomial fitting function takes the \( \log(\ ) \) of the function and restores the function with the \( \text{pow}(\ ) \) to further relieve the stress on numerical accuracy.

The simulation in figure 2 assumes the antenna output is

\[
\left( 1000(f/100)^{-2.2} + 3 + eor \right)(1 - \Gamma^2)
\]

where \( \Gamma \) is the antenna reflection coefficient from EZNEC.
The fractional signals due to scattered external noise is \( \sigma^2 G\theta/16 \) and that from receiver noise, which is assumed to be correlated with the receiver output is \( \sigma^2 \lambda \theta G\theta/(16\pi r) \)
Where

\[ \sigma = \text{reflectivity} \sim 0.1 \]

\[ G_h = \text{relative antenna gain in direction of scatter} \sim 0.01 \text{ for horizon} \]

\[ \lambda = \text{wavelength} \sim 3\text{m} \]

\[ \theta = \text{angle subtended by scatter} \]

\[ r = \text{distance to scatterer.} \]

Using these relations along with an assumed path loss of 200 dB for the forward scatter from meteor trails I obtained the following estimated of error sources.

<table>
<thead>
<tr>
<th>Source</th>
<th>Object</th>
<th>Effect</th>
</tr>
</thead>
<tbody>
<tr>
<td>Galactic noise</td>
<td>Tree 10° × 10°</td>
<td>2 ppm</td>
</tr>
<tr>
<td>“</td>
<td>Mountain 10° × 20°</td>
<td>2 ppm</td>
</tr>
<tr>
<td>Receiver noise</td>
<td>Tree at 100 m</td>
<td>4 ppm</td>
</tr>
<tr>
<td>Receiver noise</td>
<td>Mountain at 2 km</td>
<td>3 ppm</td>
</tr>
<tr>
<td>FM 100 kw</td>
<td>Moon-path loss ~240 dB</td>
<td>10 mK in 1 MHz</td>
</tr>
<tr>
<td>FM 100 kw</td>
<td>Aircraft – path loss ~210 dB 10/200 km 1m² xsect</td>
<td>10 K in 1 MHz</td>
</tr>
<tr>
<td>FM 100 kw</td>
<td>Meteors – path loss ~200 dB</td>
<td>100 K peak in 1 MHz 100 mK average</td>
</tr>
<tr>
<td>FM 100 kw</td>
<td>Sporadic E</td>
<td>Very strong- avoid daytime obs.</td>
</tr>
<tr>
<td>FM 100 kw</td>
<td>Tropospheric ducting</td>
<td>Very strong but only occasional</td>
</tr>
<tr>
<td>FM 100 kw</td>
<td>Troposcatter/conscatter ~200 dB path loss at 300 Km</td>
<td>100 K in 1 MHz but would be reduced by 30 dB more in mountain valley</td>
</tr>
<tr>
<td>Jupiter</td>
<td>~1 J at 100 MHz</td>
<td>~1 mK</td>
</tr>
</tbody>
</table>

Notes:

1] Daytime observations would be effected by the sun as well as sporadic E propagation of distant RFI.

2] Night-time only observations are preferred and those in March would be least contaminated by the Galaxy

3] The forward scattering of strong Earth based transmitters is likely to be the most serious problem.
4] One of the best locations I could find by looking at the Earth’s topography is that of Deep Springs, California. This is a deep remote valley for which the only RFI in the 100-230 MHz would be from transmitters in the valley, satellites, Meteor scatter and sporadic E. This site is about 40 miles out of the Owens Valley on route 168 and about 20 miles past CARMA on the same road. The region close to the Deep Springs lake is flat and dessert like without trees and only a few little shrubs.

5] Areas of the Earth for which FM is assigned below 80 MHz may be preferable as the meteor scatter is limited by the ionization height of about 120 km to a range of 2000 km. [If meteor scatter is really the main limitation then remote locations like the flat pacific Wake Island might be considered.]

6] Radiated receiver noise could be cancelled by using 2 identical LNAs with quadrature hybrids on input and output. However the added loss in the hybrid may degrade overall performance.

7] Typical “ping” rates for meteor scatter are about 1 per minute. At 150 MHz the typical “ping” durations is proportional to $\lambda^2$ and is about 100 ms so that the dilution factor is about 30 dB. However it should be possible to detect all the “pings” with a filter centered on the strongest FM transmitters and excise the data for the duration of the meteor burst.

8] Calibration of spectrometer would be accomplished by comparison of the sidereal variation of total power with a sky model.

References:

http://pulsar.princeton.edu/~joe/k1JT/wsJT300.pdf

www.deepsprings.edu
www.kolubus.fi/oh5iy/msobs/vhfdxpro.html